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Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Outline						







![](_page_3_Figure_0.jpeg)

- Properties
  - Rotational-vibrational spectrum.
  - Mainly three electronic-vibrational band systems between 300 nm and 400 nm: 2P(v' = 0, v''), 2P(v' = 1, v''), 1N(v' = 0, v'')
  - (Radiative) transition rate:  $\frac{1}{\tau_{v'}} = \sum_{v''} \frac{1}{\tau_{v' \to v''}} = \frac{1}{\tau_{0v'}}$
  - Constant intensity ratios between transitions within a vibrational band system.

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Collision	al Quenching					

Additional radiationless deactivation channels via collisional energy transfer

• Total transition rate: 
$$\frac{1}{\tau_{v'}} = \frac{1}{\tau_{0v'}} + \frac{1}{\tau_{cv'}}$$

- Quenching rate:  $\frac{1}{\tau_{c_{V'}}} = \sum_{x} Q_{V'}^{x}(T) \cdot n_{x} , x = N_{2}, O_{2}, Ar, H_{2}O, \dots$
- Quenching rate "constant":  $Q_{\nu'}^{x}(T) \propto \sqrt{T}$  ( $\rightarrow$  kinetic gas theory)

• Number density: 
$$n_x = \frac{p_x}{kT} = \frac{f_x}{kT} \cdot p$$

## Total transition rate

$$\frac{1}{\tau_{v'}} = \frac{1}{\tau_{0v'}} \cdot \left(1 + p \cdot \underbrace{\frac{\tau_{0v'}}{kT} \sum_{x} f_x \cdot Q_{v'}^x(T)}_{1/p'_{v'}}\right)$$

 $\parallel$ 

→ linear pressure-dependence for constant mixing ratios and temperatures.

![](_page_5_Figure_0.jpeg)

$$Y_{\nu',\nu''}(E,p,T) = Y_{\nu'}^0(E) \cdot R_{\nu',\nu''} \cdot \frac{\tau_{\nu'}(p,T)}{\tau_{0\nu'}} \qquad \left[ \frac{photons}{dep.\ energy} \right]$$

![](_page_5_Figure_2.jpeg)

![](_page_6_Figure_0.jpeg)

$$Y_{v',v''}(E,\rho,T) = Y_{v'}^{0}(E) \cdot R_{v',v''} \cdot \frac{\tau_{v'}(\rho,T)}{\tau_{0\,v'}} \qquad \left[\frac{\text{photons}}{\text{dep. energy}}\right]$$

![](_page_6_Figure_3.jpeg)

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Fluoresc	ence Yield					

$$Y_{v',v''}(E,p,T) = Y_{v'}^{0}(E) \cdot R_{v',v''} \cdot \frac{\tau_{v'}(p,T)}{\tau_{0,v'}} \qquad \left[\frac{photons}{dep.\ energy}\right]$$

![](_page_7_Figure_3.jpeg)

![](_page_8_Figure_0.jpeg)

$$Y_{v',v''}(E,p,T) = Y_{v'}^{0}(E) \cdot R_{v',v''} \cdot \frac{\tau_{v'}(p,T)}{\tau_{0,v'}}$$

![](_page_8_Figure_3.jpeg)

photons dep. energy

![](_page_9_Figure_0.jpeg)

$$Y_{v',v''}(E,p,T) = Y_{v'}^{0}(E) \cdot R_{v',v''} \cdot \frac{\tau_{v'}(p,T)}{\tau_{0,v'}}$$

 $\left[ \frac{photons}{dep. energy} 
ight]$ 

# Ingredients Intrinsic fluorescence yield of most intensive transition: $Y_{V'}^0(E)$ $\begin{bmatrix} photons \\ dep. \ energy \end{bmatrix}$ Constant intensity ratios $R_{V',V''}$ relative to most intensive transition. Fraction of radiative transitions: $\frac{\tau_{V'}(p,T)}{\tau_{0V'}} = \frac{1/\tau_{0V'}}{1/\tau_{V'}(p,T)} = \frac{radiative \ rate}{total \ rate}$

### Advantages of this representation

- Consistent description.
- Clear meaning of parameters.
- Does not depend on energy loss function (Bethe-Bloch or similar).

![](_page_10_Figure_0.jpeg)

$$Y_{v',v''}(E,p,T) = Y_{v'}^{0}(E) \cdot R_{v',v''} \cdot \frac{\tau_{v'}(p,T)}{\tau_{0,v'}}$$

photons dep. energy

### Ingredients

• Intrinsic fluorescence yield of most intensive transition:  $Y_{V'}^0(E)$   $\left[\frac{photons}{dep. \, energy}\right]$ 

- Constant intensity ratios  $R_{v',v''}$  relative to most intensive transition.
- Fraction of radiative transitions:  $\frac{\tau_{V'}(\rho,T)}{\tau_{0_{V'}}} = \frac{1/\tau_{0_{V'}}}{1/\tau_{v'}(\rho,T)} = \frac{\text{radiative rate}}{\text{total rate}}$

⇒ All these parameters have been measured with the AirLight-Experiment ...

![](_page_11_Picture_0.jpeg)

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Setup of	the AirLight Exp	periment				

![](_page_12_Figure_1.jpeg)

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Setup of	the AirLight Exp	periment				

![](_page_13_Figure_1.jpeg)

![](_page_14_Figure_0.jpeg)

![](_page_15_Figure_0.jpeg)

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Aco	uisition					

![](_page_16_Figure_1.jpeg)

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Aco	quisition					

![](_page_17_Figure_1.jpeg)

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Aco	quisition					

![](_page_18_Figure_1.jpeg)

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

	Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Acquisition	Data Aco	quisition					

![](_page_19_Figure_1.jpeg)

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

![](_page_20_Figure_0.jpeg)

![](_page_20_Figure_1.jpeg)

Pressure

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

Motivation Fluorescence	Model AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Acquisition					

![](_page_21_Figure_1.jpeg)

Pressure

Temperature

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Acc	uisition					

![](_page_22_Figure_1.jpeg)

Pressure

Temperature

Measurement of coincidences between electron- and photon-detectors:

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

![](_page_22_Figure_9.jpeg)

**Relative Humdity** 

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Acq	uisition					

![](_page_23_Figure_1.jpeg)

**Relative Humdity** 

Free PMT rates

Measurement of coincidences between electron- and photon-detectors:

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Data Acq	uisition					

![](_page_24_Figure_1.jpeg)

![](_page_24_Figure_2.jpeg)

**Relative Humdity** 

Free PMT rates

- Pulse height distributions.
- Difference-time spectra.
- Absolute scaler values.
- Coincident/free electron energy spectra.

- Pressure.
- Temperature.
- Relative Humidity.
- Free/Coincident event rates.
- High Voltage/Current.

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Simula	ation					

![](_page_25_Figure_1.jpeg)

GEANT4 Simulation (version 7.1) to determine:

- Electron energy spectra.
- Energy deposit in chamber.
- Photon angle distribution.
- Acceptance of photomultipliers.

![](_page_26_Figure_0.jpeg)

![](_page_26_Figure_1.jpeg)

![](_page_26_Figure_2.jpeg)

![](_page_26_Figure_3.jpeg)

![](_page_26_Figure_4.jpeg)

![](_page_27_Figure_0.jpeg)

0.0

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# Important note

![](_page_27_Figure_2.jpeg)

Measured energy spectrum is very much affected by multiple- or back-scattering effects in the collimator and in the gas!

1000

 $\frac{dN}{d\varepsilon} \propto \eta \cdot \varepsilon \cdot (\varepsilon_0 - \varepsilon)^2 \cdot F(Z, \eta) \cdot C(Z, \eta)$ 

1000

⇒ To obtain reasonable results the facrange parameter of the multiple scattering model has to be lowered to 0.01!

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Measurement of the Air Fluorescence Yield with the AirLight Experiment

0 000

 ${}^{90}_{38}\text{Sr} \xrightarrow{t_{1/2} = 29 \text{ a}} {}^{90}_{39}\text{Y} \xrightarrow{t_{1/2} = 64 \text{ h}} {}^{90}_{40}\text{Zr}$ 

1500 2000 Enerav [keV] Tilo Waldenmaie

1500 2000 Electron Energy [keV]

# Energy deposit in chamber

![](_page_28_Figure_8.jpeg)

![](_page_29_Figure_0.jpeg)

![](_page_30_Figure_0.jpeg)

6

![](_page_30_Figure_1.jpeg)

![](_page_30_Figure_2.jpeg)

• Measurement of <sup>22</sup>Na Compton-spectrum  $\frac{dN}{dE}(E)$ .

• Convolution: 
$$\frac{dN}{dE}(E) = \frac{dN_{bare}}{dE}(E) \otimes G(E, \sigma_E(E))$$

• 
$$\mathsf{E} = \mathsf{a} + \mathsf{b} \cdot \mathsf{ADC}$$
,  $\sigma_\mathsf{E}(\mathsf{E}) = \sqrt{\sigma_\mathsf{ped}^2 + \mathsf{c} \cdot \mathsf{E}}$ 

 Calibration constants a, b, c from fit to measured spectrum.

• Typical energy resolution: 
$$\frac{\sigma_{\rm E}}{{\rm E}} \sim 10 \ \% \cdot \sqrt{\frac{1000 \ {\rm keV}}{{\rm E}}}$$

Idea: Why not use the <sup>90</sup>Sr-energy spectrum as reference spectrum?

Problem: Spectral shape at scintillator unknown due to scattering/energy loss in the chamber. Solution: Simulate energy spectra at scintillator for different pressures (with *facrange* < 0.01).

![](_page_31_Figure_3.jpeg)

- Individual calibration of each run.
- Minimizing run-to-run fluctuations.

MC method

1000 1200 1400 160

800

![](_page_32_Figure_0.jpeg)

# **Relative Calibration of the Photomultipliers**

![](_page_32_Figure_2.jpeg)

![](_page_32_Figure_3.jpeg)

![](_page_32_Figure_4.jpeg)

Detected photons:  $N_{det} = \varepsilon_{\Omega} \cdot \varepsilon_{s} \cdot f_{cal} \cdot N_{0}$ 

• 
$$\varepsilon_{s} = \int_{\lambda} \varepsilon_{QE}^{0}(\lambda) \cdot T(\lambda) \cdot \frac{dN}{d\lambda} d\lambda = const.$$

- ۰ Photoelectron cut:  $0.5 \le p.e. \le 2.0$ (for calibration and measurement)
- ۰ Calibration relative to channel 3 ( $f_{cal} \equiv 1$ )

![](_page_33_Figure_0.jpeg)

![](_page_34_Figure_0.jpeg)

![](_page_34_Figure_1.jpeg)

Estimation of absolute uncertainty:

- Discriminator threshold assumed to be stable.
- Events above 2 pe are mostly background.
- 12 % of the events are between discr. threshold and 0.5 pe.
- Less than 15 % of the events are below discr. threshold.

 $\Rightarrow N_{abs} = (1 + 12\% + 7.5\% \pm 7.5\%) \cdot N_{rel} = (1.195 \pm 0.075) \cdot N_{rel}$ 

Normalization error of QE-curve assumed to be  $\sim$  10%:

 $\Rightarrow \text{ Calibration constant: } C_{abs} = (1 \pm 0.1) \cdot \frac{N_{abs}}{N_{rel}} = 1.195 \pm 0.141 \quad , \quad \frac{\Delta C_{abs}}{C_{abs}} = 12\%$ 

![](_page_35_Figure_0.jpeg)

![](_page_35_Figure_1.jpeg)

Estimation of absolute uncertainty:

Final absolute accuracies

 $\Rightarrow$  Absolute accuracy of single bands  $\lesssim$  15 %

• Reduction to  $\leq$  10 % in future possible with calibration by Rayleigh scattering.

 $\Rightarrow N_{abs} = (1 + 12\% + 7.5\% \pm 7.5\%) \cdot N_{rel} = (1.195 \pm 0.075) \cdot N_{rel}$ 

Normalization error of QE-curve assumed to be  $\sim$  10%:

$$\Rightarrow \text{ Calibration constant: } C_{abs} = (1 \pm 0.1) \cdot \frac{N_{abs}}{N_{rel}} = 1.195 \pm 0.141 \quad , \quad \frac{\Delta C_{abs}}{C_{abs}} = 12\%$$

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary	
Measurements & Data Analysis							

The complete dataset used for the analysis consists of  $\sim$  50 runs with:

- Pure nitrogen
- Dry air (78% N<sub>2</sub>, 21% O<sub>2</sub>, 1% Ar)
- Mixture (90% N<sub>2</sub>, 10% O<sub>2</sub>)
- Nitrogen + water vapor
- Temperature:  $\sim 20^{\circ}C$
- Pressure range: 2 hPa 1000 hPa
- Duration: 12 h 30 h (depending on gas and pressure)

Analysis philosophy:

- Step 1: Determination of quenching parameters and intensity ratios over whole energy range ( $\rightarrow$  max. statistics).
- Step 2: Determination of intensities (intrinsic yields) with fixed parameters of step 1 for energy sub-ranges.

Motivation

Summary

Analysis

# Step 1: Determination of Quenching Parameters and Intensity Ratios

![](_page_37_Figure_7.jpeg)

# Problem

Overlapping bands within a single filter channel.

# Solution

- Global analysis of all datasets (~ 50 runs).
- Constrained χ<sup>2</sup>-minimization with minimal set of parameters.
- Physical constraints for transitions from same vibrational level v':
- $\rightarrow$  Same intrinsic lifetime  $\tau_{0v'}$ .
- $\rightarrow$  Same quenching rate constants  $Q_{v'}^{\chi}$ .
- $\rightarrow$  Same intrinsic yield  $Y_{\nu'}^0$ .
- $\rightarrow$  Constant Intensity ratios  $R_{\nu',\nu''}$ .

Calibration

Analysis Summary

# Time Spectra in Nitrogen at 20 hPa

![](_page_38_Figure_7.jpeg)

Calibratio

Summary

# Time Spectra in Nitrogen at 100 hPa

![](_page_39_Figure_8.jpeg)

![](_page_40_Figure_0.jpeg)

![](_page_41_Figure_0.jpeg)

 Good relative description of the total fluorescence yield over whole pressure range within 4 %.

![](_page_42_Figure_1.jpeg)

![](_page_42_Figure_2.jpeg)

![](_page_42_Figure_3.jpeg)

Additional constraint for lines:

$$\frac{1}{\tau_{v'}} = \frac{1}{\tau_{0v'}} \cdot \left(1 + p \cdot \underbrace{\frac{\tau_{0v'}}{kT} \sum_{x} f_x \cdot Q_{v'}^x(T)}_{1/p'(T)}\right)$$

 Fit to 1N(0,0) data yields only reasonable results under this condition.

![](_page_43_Figure_1.jpeg)

![](_page_44_Figure_0.jpeg)

Measurements with pure nitrogen at 30 hPa plus a variable amount of water vapor.

Res	ults	
-		$Q_{H_2O} [10^{-10} cm^3 s^{-1}]$
-	2P(0,v")	$5.43\pm0.12$
	2P(1,v")	$5.78\pm0.17$
	1N(0,v")	$16.02\pm1.09$

Large quenching rate constant of 1N system due to polar character of ionized nitrogen?

 Motivation
 Fluorescence Model
 AirLight Experiment
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 Analysis
 Summary

 Step 2: Energy Dependence of Intrinsic Yield
 Step 2
 Step

Re-analyzing sub-samples of 250 keV energy intervals with fixed quenching parameters and intensity ratios.

![](_page_45_Figure_2.jpeg)

- Determination of deposited energy from GEANT4 simulations.
- No energy dependence of  $Y_{\nu'}^0(E)$  in investigated range.
- $\Rightarrow$  Number of photons is proportional to ionization energy loss.

![](_page_46_Figure_0.jpeg)

![](_page_46_Figure_1.jpeg)

![](_page_47_Figure_0.jpeg)

![](_page_47_Figure_1.jpeg)

![](_page_48_Figure_0.jpeg)

![](_page_48_Figure_1.jpeg)

Motivation	Fluorescence Model	AirLight Experiment	Simulation	Calibration	Analysis	Summary
Summa	ıry					
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### Achieved so far ...

- Nitrogen fluorescence spectrum can be sub-divided into several (three) sub-spectra.
- Transitions of a sub-spectrum are connected by several relations.
- Fluorescence spectrum has been measured with the AirLight-Experiment and analyzed according to these relations.
- Global fit leads to consistent description of fluorescence yield with a minimal set of parameters.
- Fluorescence yield does not depend on energy.
- Absolute uncertainties of single nitrogen bands  $\leq$  15 %.

### Still to do ...

- Further reduction of absolute uncertainties down to  $\sim$  10 %.
- Quantification of water vapor influence on shower reconstruction.

Ph.D. Thesis: http://www.auger.de/interna/docs/repository/FZKA7209\_Report.pdf