

WPCF, Kroměříž, August 2005

Non-Gaussian Effects in Identical Pion Correlation Function at STAR

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August 16, 2005

Outline

- Motivation
- STAR data
- Event and Track selection
- Identical π - π correlation function
- Bowler-Sinyukov fit to data
- Levy source distribution fit
- Edgeworth expansion
- Summary

Motivation

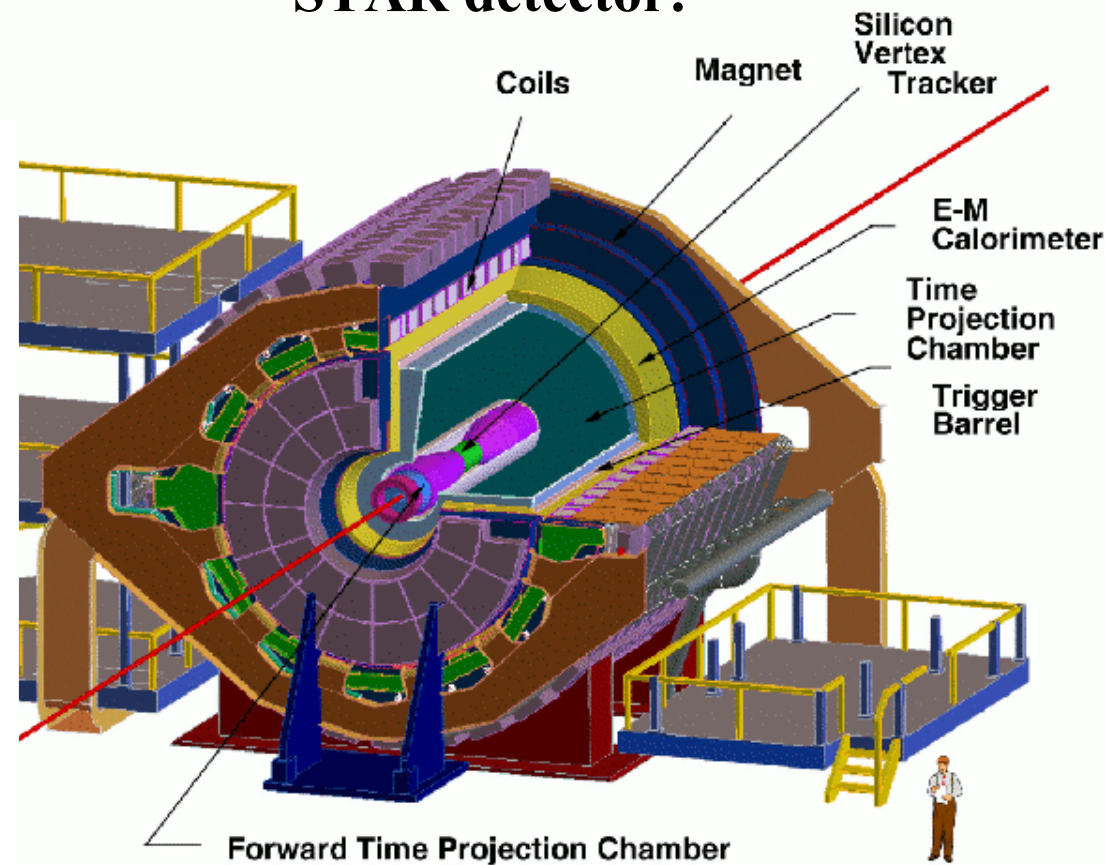
- Why do we care about non-Gaussian issue?
 - Source distribution function is in most models non-Gaussian and standard methods of fitting experimental CF assume Gaussian source.
 - Need to parametrize source properly in order to minimize systematic errors.
- Possible methods of studying the non-Gaussian effects of CF include:
 - Source imaging, see talk by P.Danielewicz, P.Chung, D.Brown
 - Spherical harmonics, see talk by Z.Chajęcki
 - Levy stable source distribution, see talk by T.Csörgő
 - Edgeworth expansion

STAR data

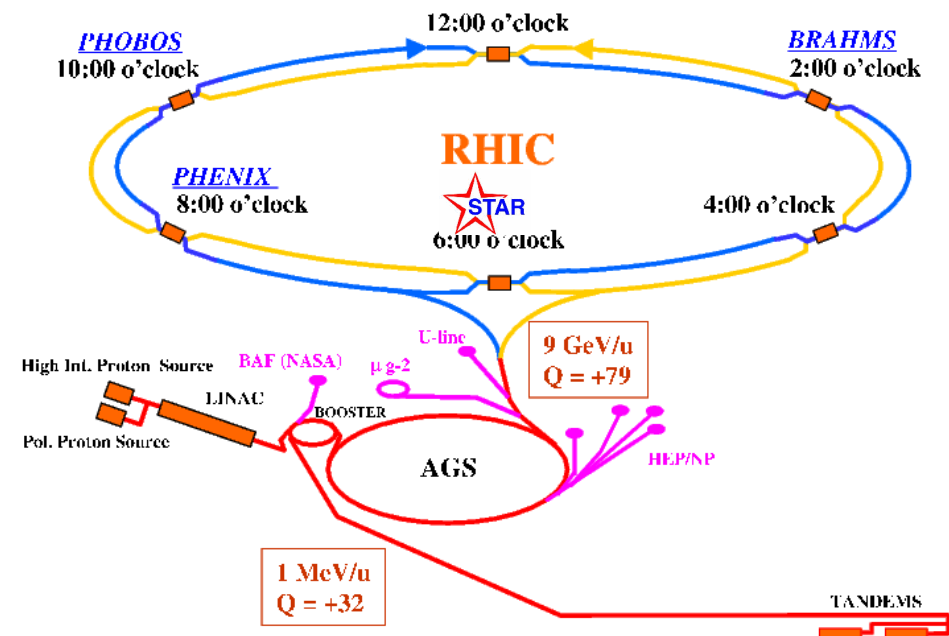
- Au+Au collisions at energy $\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$
- Year 2004 data, Full Field (0.5 T)
- $\sim 11 \text{ M}$ MinBias events



STAR detector:

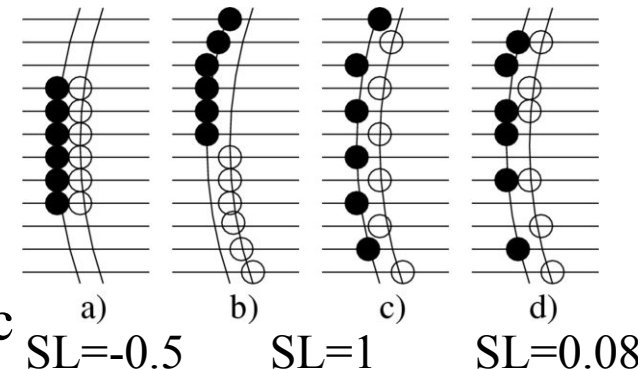
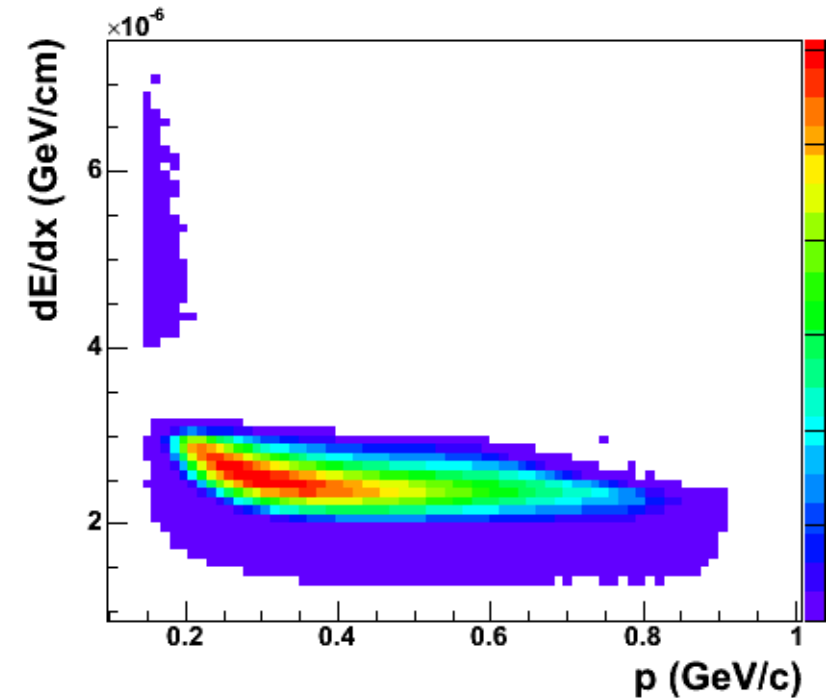


RHIC complex at BNL:

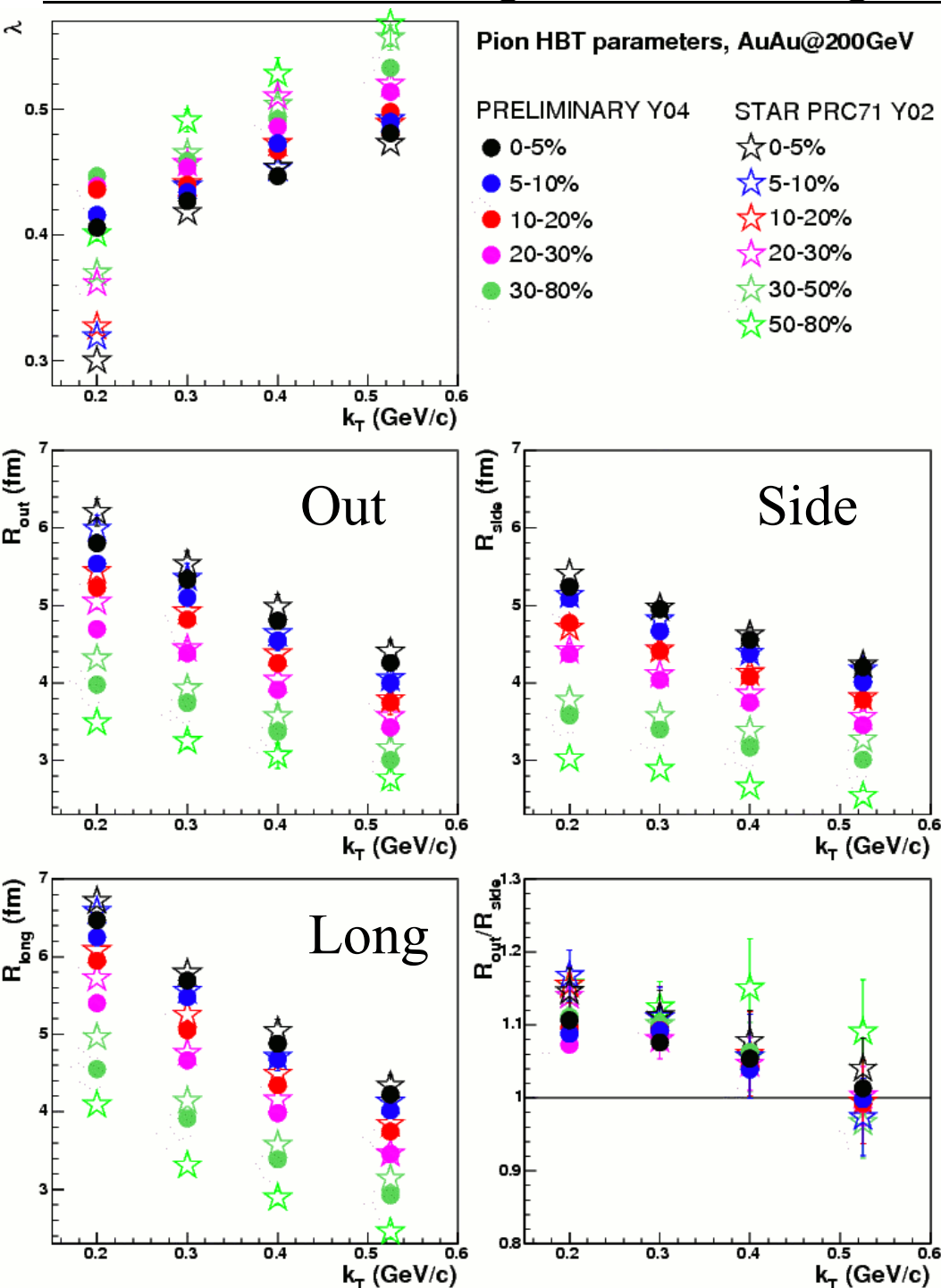


Event and Track selection

- Same cuts as in STAR, Phys. Rev. C 71 (2005) 044906
- Event cuts:
 - Centrality binning {0-5, 5-10, 10-20, 20-30, 30-80} %
 - $z_{\text{Vertex}} \pm 25$ cm
- Track cuts:
 - pion dE/dx band ± 2 s
 - remove dE/dx electron band
 - $p_T = \{0.15, 0.80\}$ GeV/c
 - $y = \{-0.5, 0.5\}$
- Pair cuts:
 - Id: $\pi^+ - \pi^+$, $\pi^- - \pi^-$
 - anti-splitting ($-0.5 < SL < 0.6$)
 - anti-merging (max. 5 % merged)
 - $k_T = \{0.15-0.25, 0.25-0.35, 0.35-0.45, 0.45-0.60\}$ GeV/c



Comparison to published STAR data



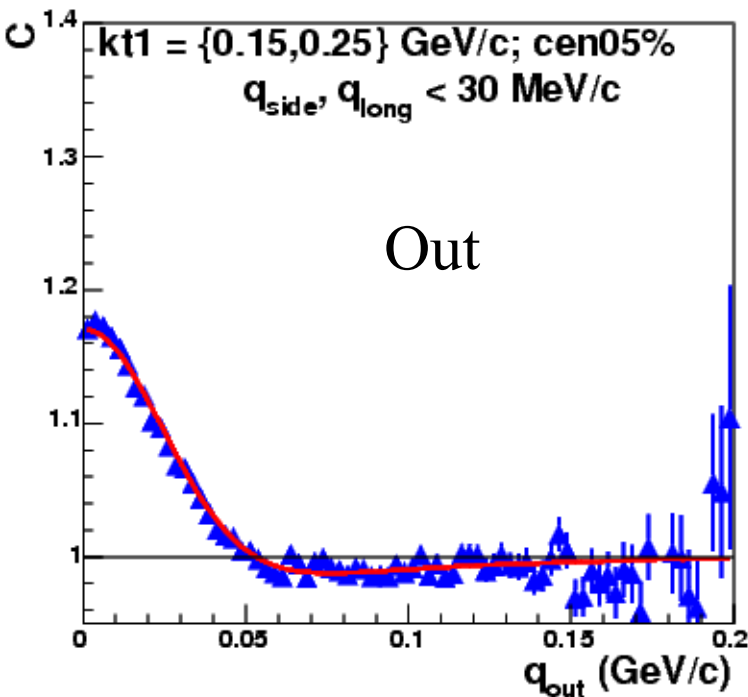
- Bowler-Sinyukov fit to data

$$C(q) = (1 - \lambda) + \lambda K_c (1 + \exp(-\sum R_{ij}^2 q_i q_j))$$

- 3D identical pion CF is fit using the Bertsch-Pratt parametrization in LCMS frame without crossterms in azimuthally integrated analyses
- No momentum resolution correction yet

- Radii are consistent within errors with published STAR PRC71 data
- Difference in lambda in the lowest k_T bin explained by improved purity of pion sample

Identical π - π correlation function



Identical $\pi\pi$ CF

▲ Data - PRELIMINARY

— Bowler-Sinyukov fit

$$\lambda = 0.406 \pm 0.002$$

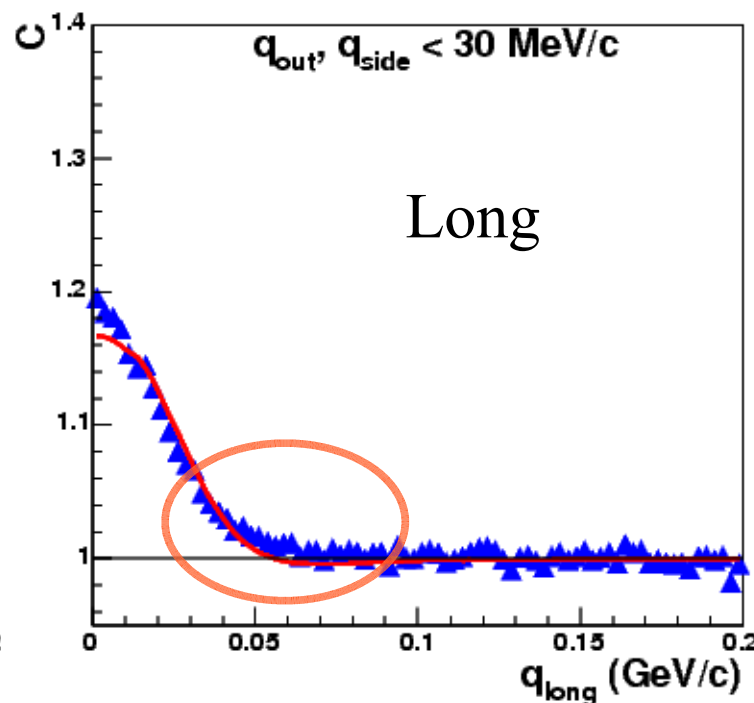
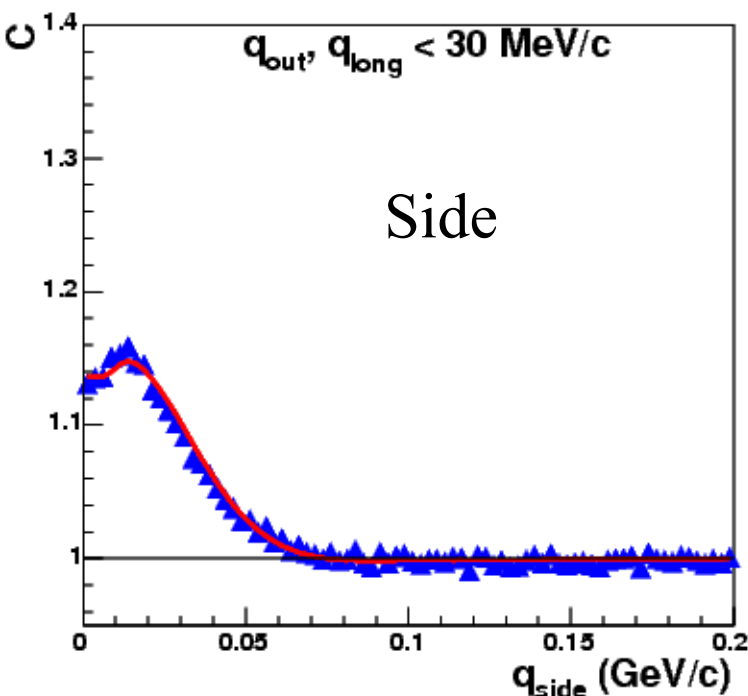
$$R_{\text{out}} = 5.80 \pm 0.04 \text{ fm}$$

$$R_{\text{side}} = 5.24 \pm 0.03 \text{ fm}$$

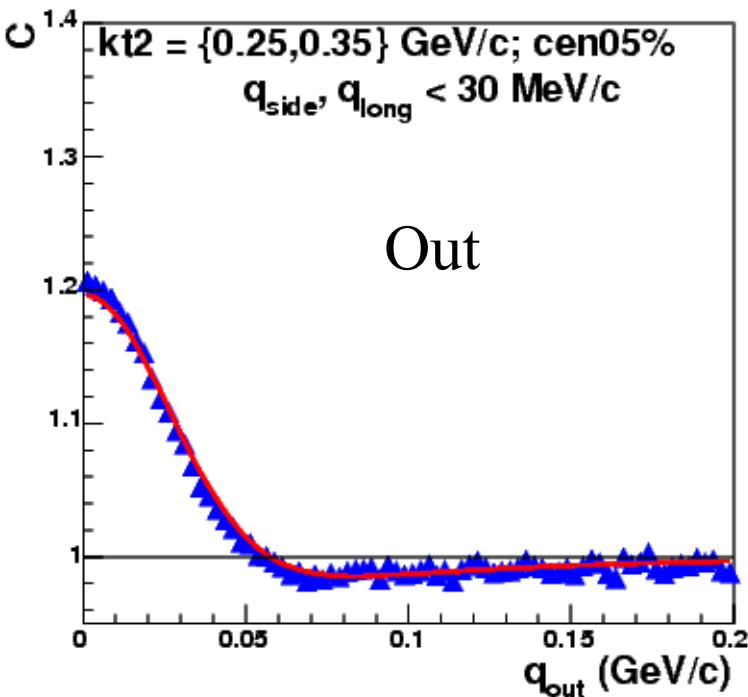
$$R_{\text{long}} = 6.47 \pm 0.03 \text{ fm}$$

$$\chi^2/\text{NDF} = 1.11750$$

- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- Non-Gaussian shape mostly visible in long direction



Identical π - π correlation function



Identical $\pi\pi$ CF

▲ Data - PRELIMINARY

— Bowler-Sinyukov fit

$$\lambda = 0.427 \pm 0.002$$

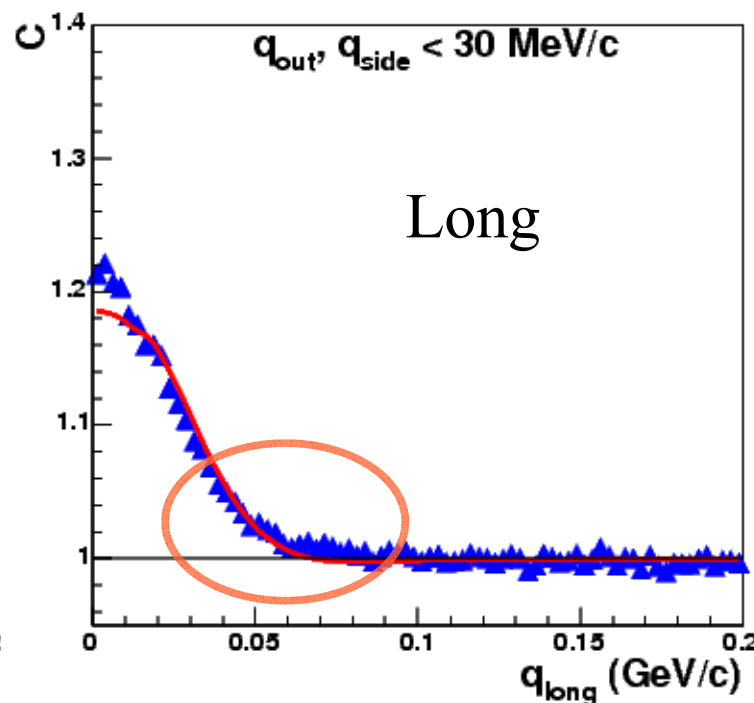
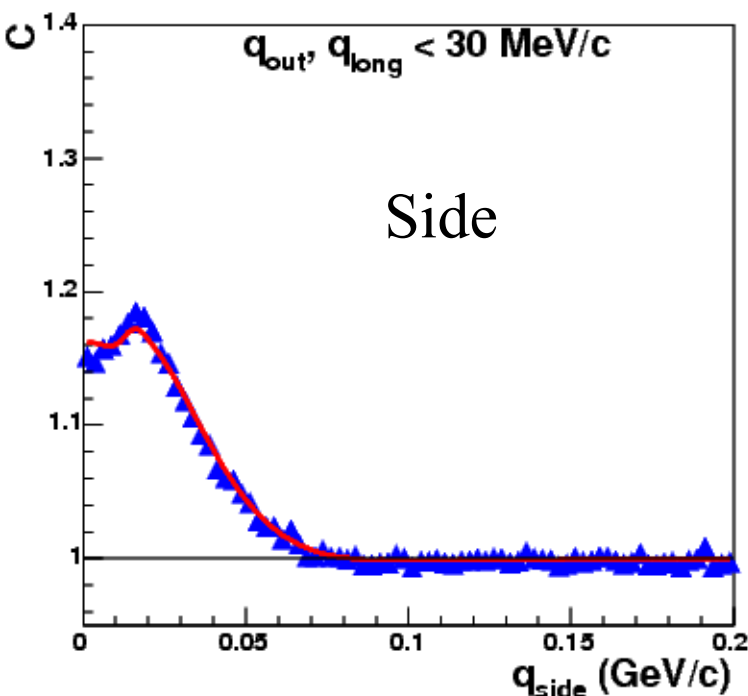
$$R_{\text{out}} = 5.33 \pm 0.02 \text{ fm}$$

$$R_{\text{side}} = 4.95 \pm 0.02 \text{ fm}$$

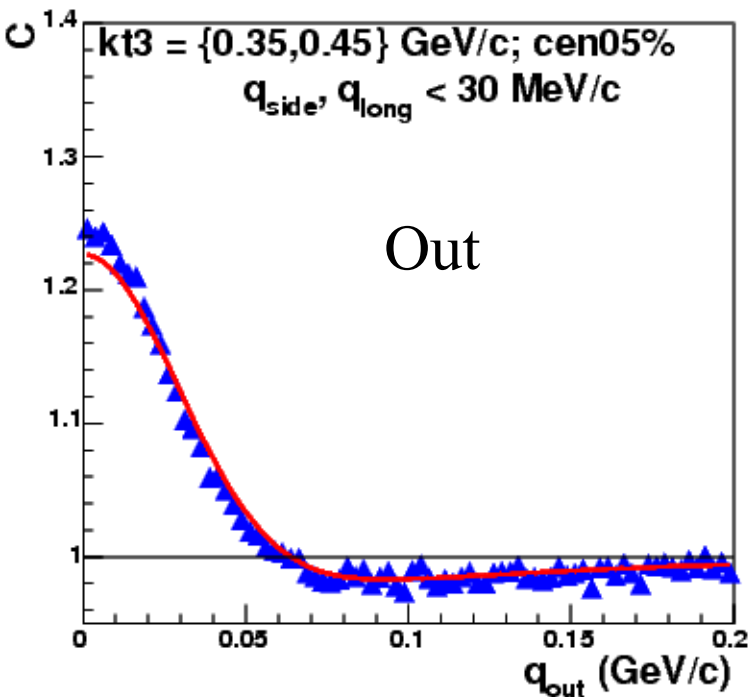
$$R_{\text{long}} = 5.69 \pm 0.03 \text{ fm}$$

$$\chi^2/\text{NDF} = 1.11024$$

- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- Non-Gaussian shape mostly visible in long direction



Identical π - π correlation function



Identical $\pi\pi$ CF

▲ Data - PRELIMINARY

— Bowler-Sinyukov fit

$$\lambda = 0.447 \pm 0.003$$

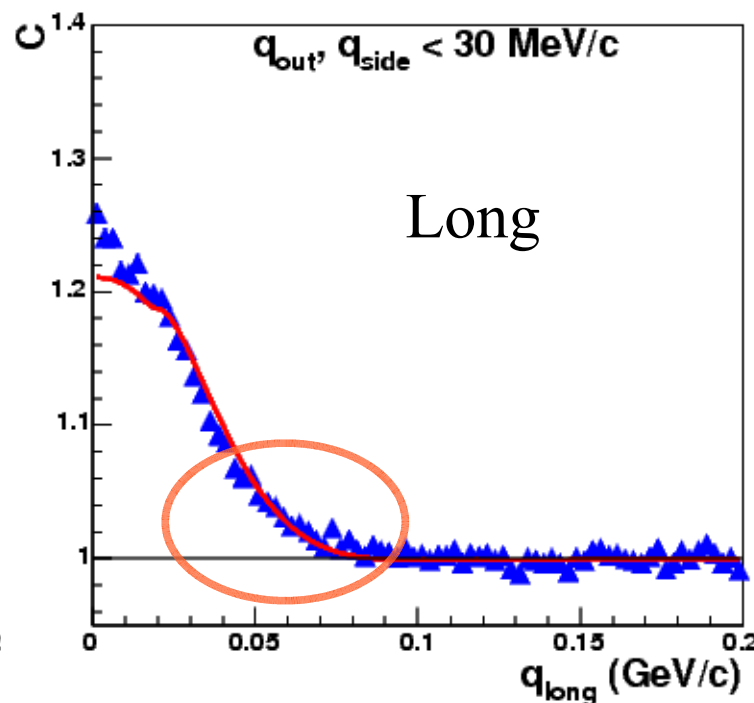
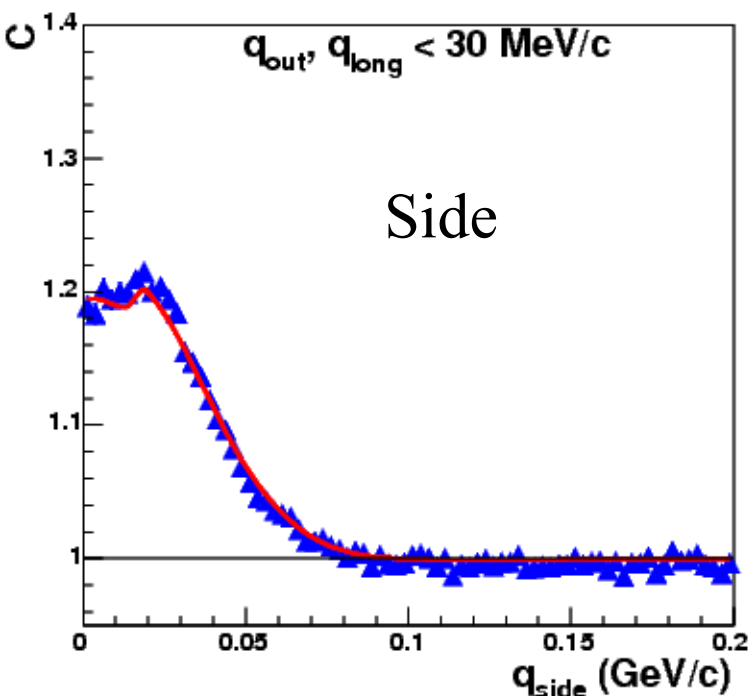
$$R_{\text{out}} = 4.80 \pm 0.03 \text{ fm}$$

$$R_{\text{side}} = 4.56 \pm 0.02 \text{ fm}$$

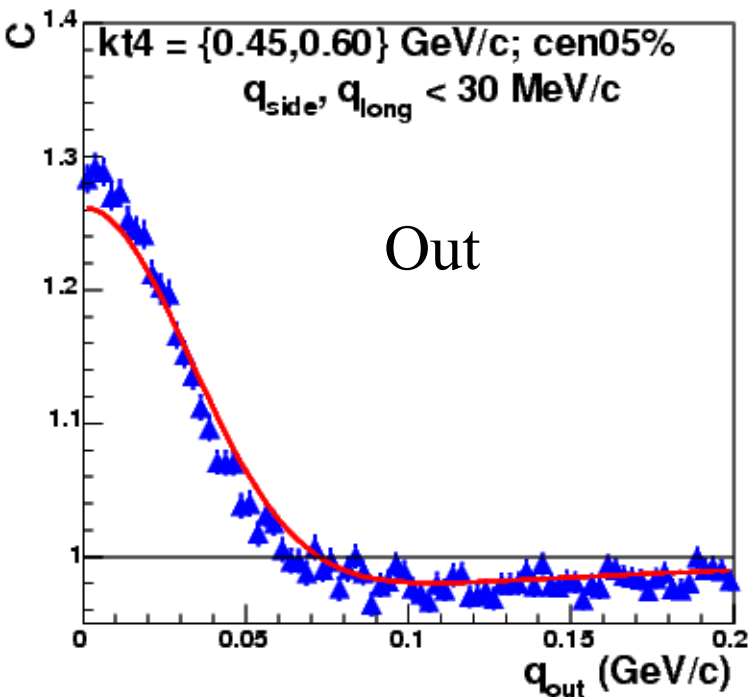
$$R_{\text{long}} = 4.88 \pm 0.02 \text{ fm}$$

$$\chi^2/\text{NDF} = 1.11285$$

- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- Non-Gaussian shape mostly visible in long direction



Identical π - π correlation function



Identical $\pi\pi$ CF

▲ Data - PRELIMINARY

— Bowler-Sinyukov fit

$$\lambda = 0.481 \pm 0.006$$

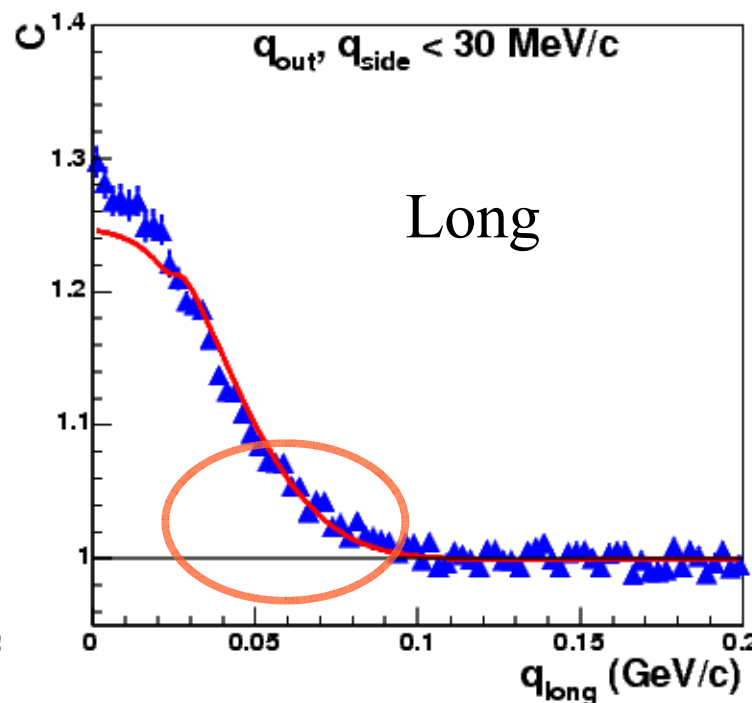
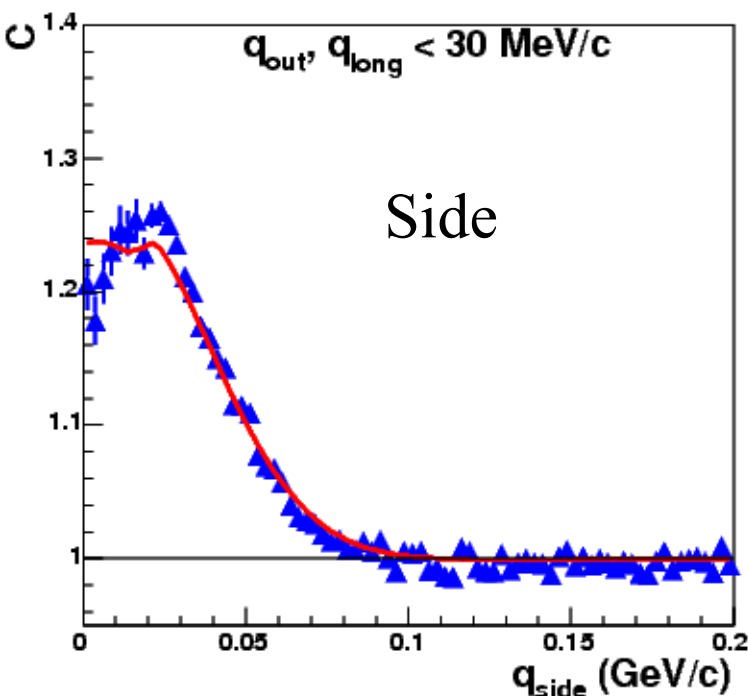
$$R_{\text{out}} = 4.26 \pm 0.03 \text{ fm}$$

$$R_{\text{side}} = 4.20 \pm 0.03 \text{ fm}$$

$$R_{\text{long}} = 4.22 \pm 0.03 \text{ fm}$$

$$\chi^2/\text{NDF} = 1.12314$$

- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- Non-Gaussian shape mostly visible in long direction



Levy source distribution fit

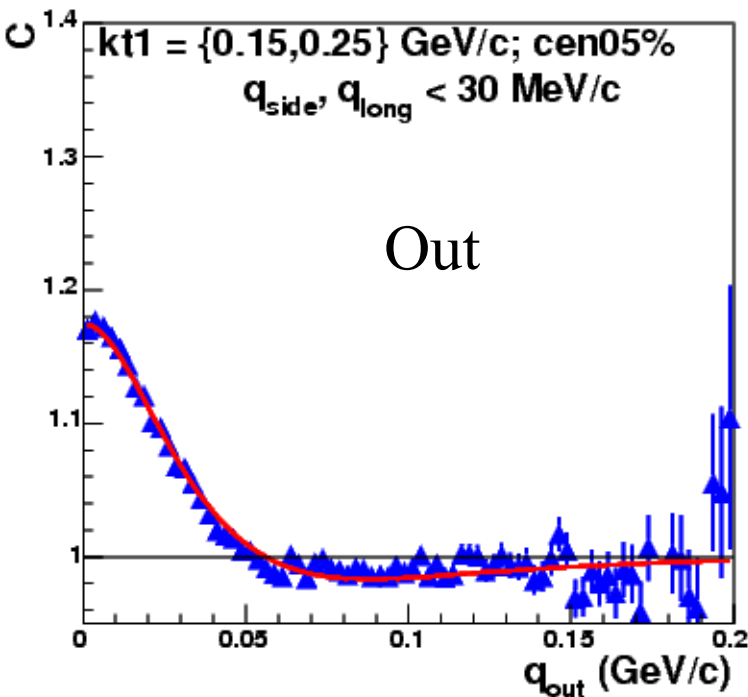
- T.Csörgő, *et al.*: Bose-Einstein correlations for Levy stable source distributions, Eur.Phys.J. C36(2004)67
- The general form of two-particle BECF
$$C(q)=1+\lambda \exp(-(\sum R_{ij}^2 q_i q_j)^{\alpha/2})$$
- $0 < \alpha \leq 2$...Levy index of stability
- $\alpha < 2$...CF becomes more peaked than a Gaussian and it develops longer tails

- Taking into account the Coulomb effect, Levy source distribution fit to data

$$C(q)=(1-\lambda)+\lambda K_c(1+\exp(-(\sum R_{ij}^2 q_i q_j)^{\alpha/2}))$$

- Using Bertsch-Pratt parametrization in LCMS frame, asimuthally integrated analyses, $R_{ij}=0$ $i \neq j$

Levy fit to identical π - π correlation function



Identical $\pi\pi$ CF

▲ Data - PRELIMINARY

— Bowler-Sinyukov fit (Levy)

$$\lambda = 0.776 \pm 0.007$$

$$R_{\text{out}} = 7.61 \pm 0.05 \text{ fm}$$

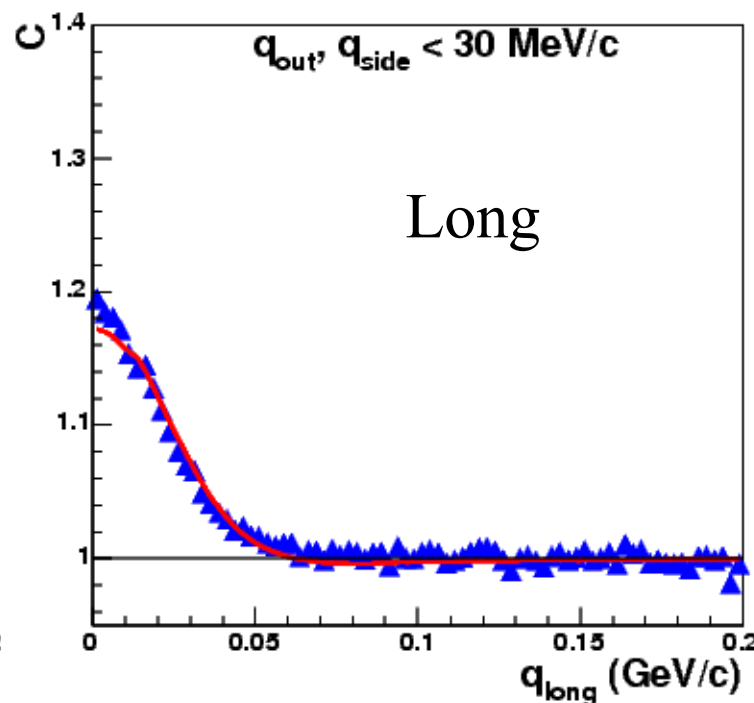
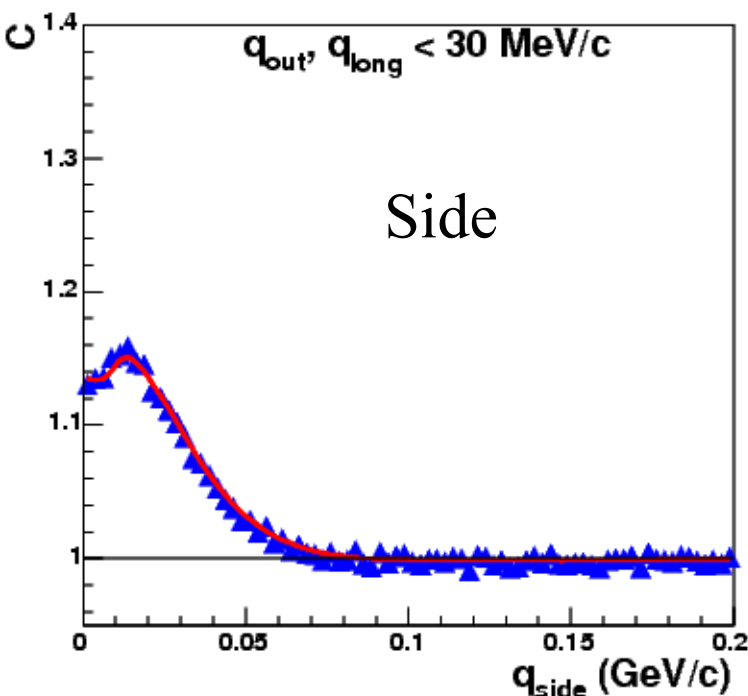
$$R_{\text{side}} = 7.64 \pm 0.05 \text{ fm}$$

$$R_{\text{long}} = 9.05 \pm 0.05 \text{ fm}$$

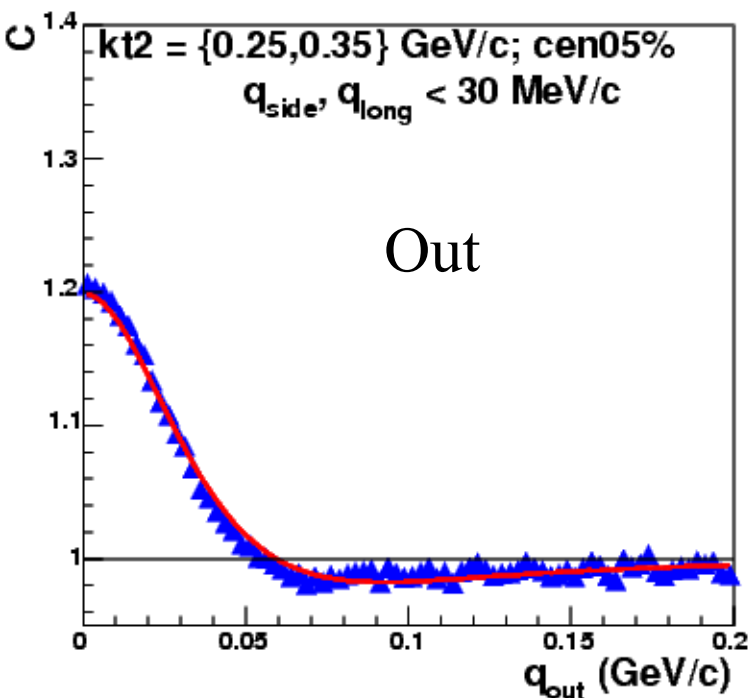
$$\alpha = 1.261 \pm 0.006$$

$$\chi^2/\text{NDF} = 1.11497$$

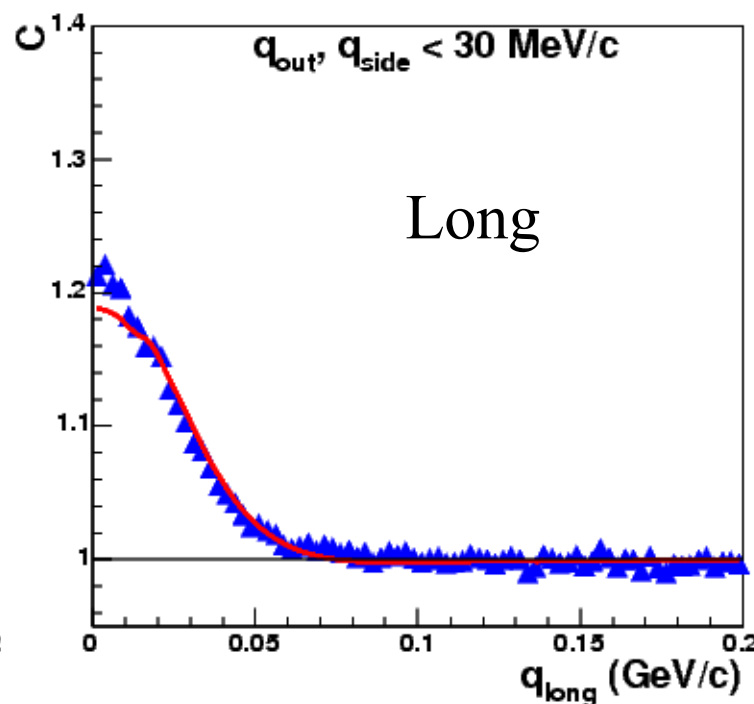
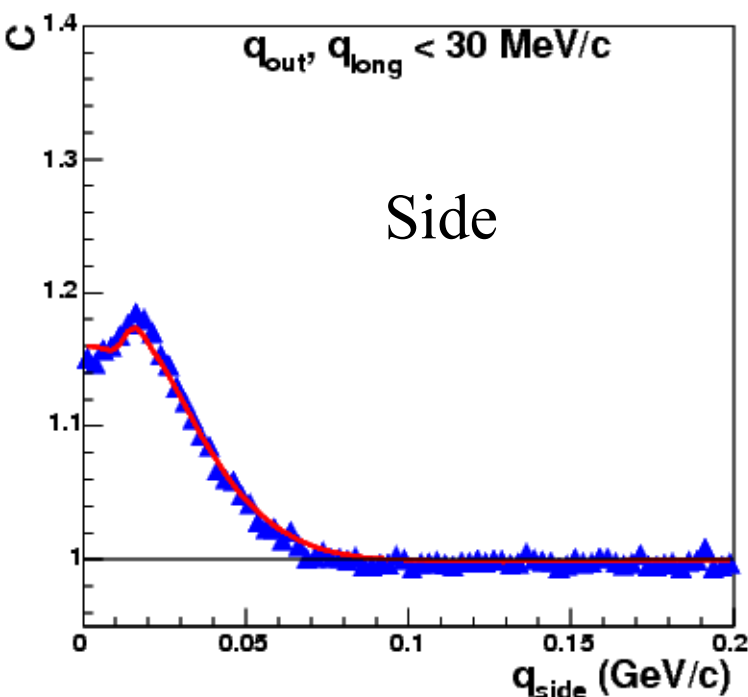
- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- α parameter increases with k_T
- $\alpha < 2$



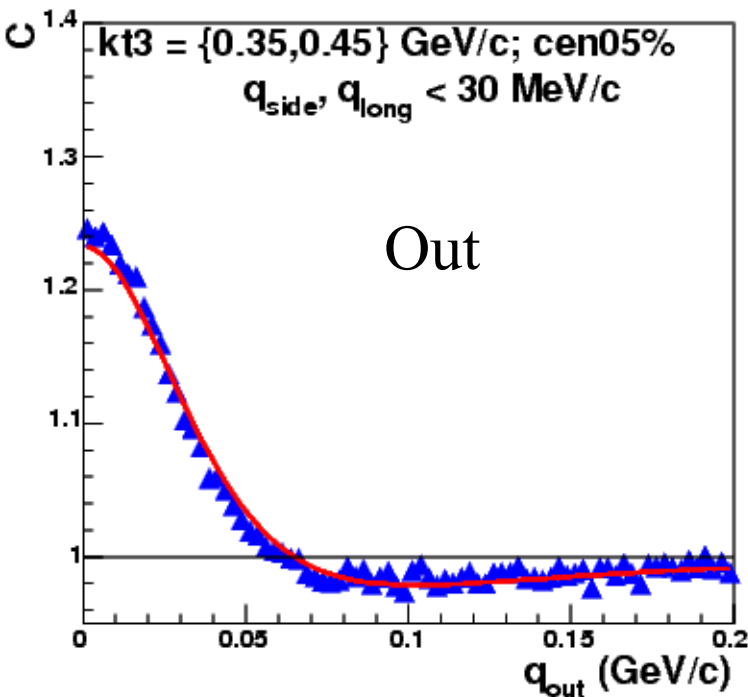
Levy fit to identical π - π correlation function



- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- α parameter increases with k_T
- $\alpha < 2$



Levy fit to identical $\pi\pi$ correlation function



Identical $\pi\pi$ CF

▲ Data - PRELIMINARY

— Bowler-Sinyukov fit (Levy)

$$\lambda = 0.633 \pm 0.005$$

$$R_{\text{out}} = 5.54 \pm 0.03 \text{ fm}$$

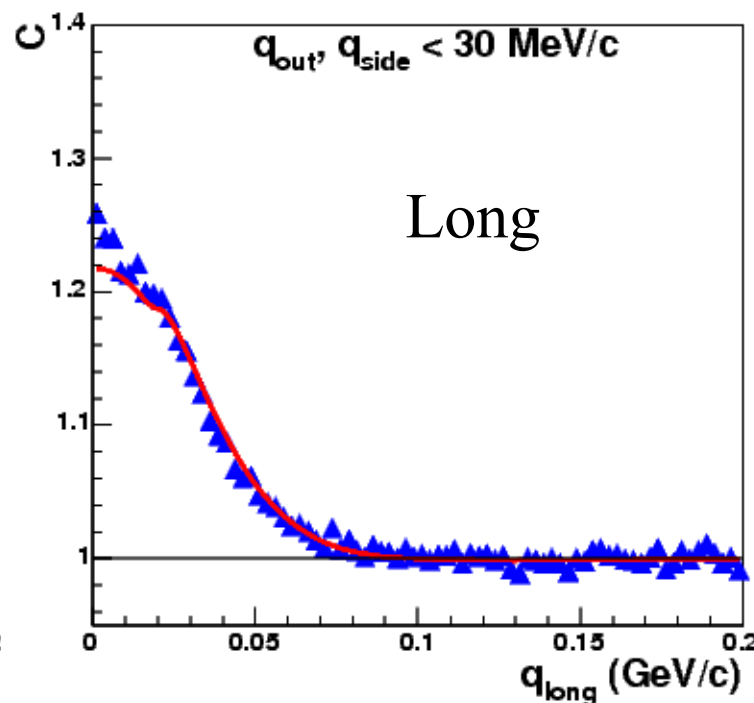
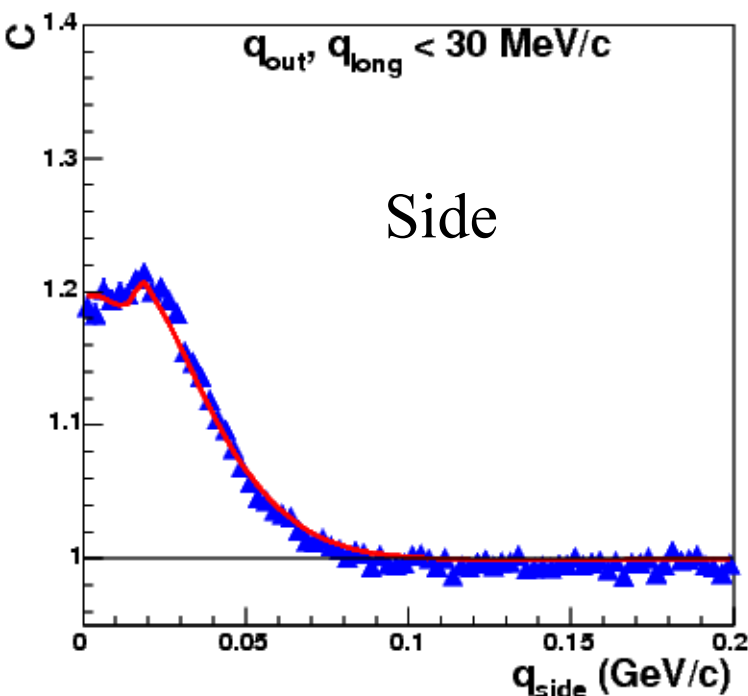
$$R_{\text{side}} = 5.57 \pm 0.03 \text{ fm}$$

$$R_{\text{long}} = 5.91 \pm 0.03 \text{ fm}$$

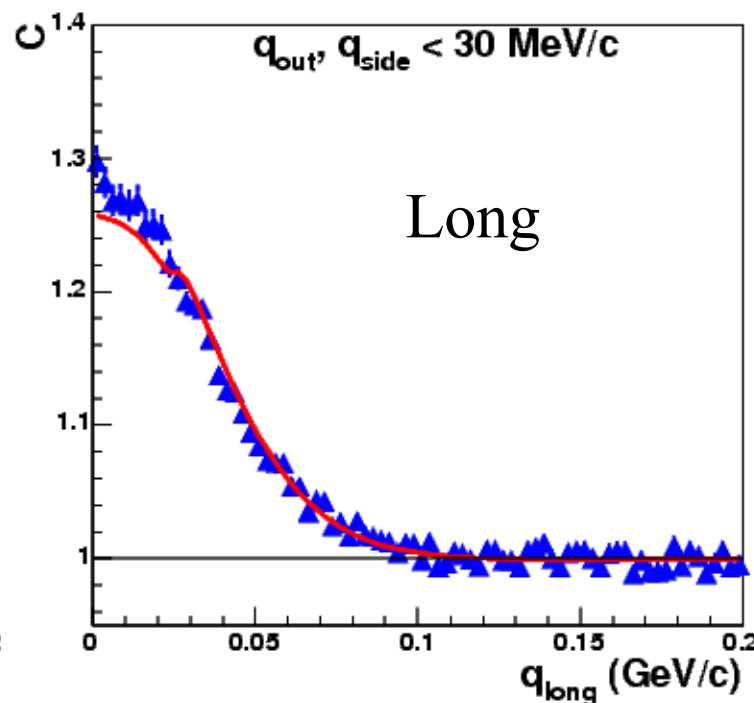
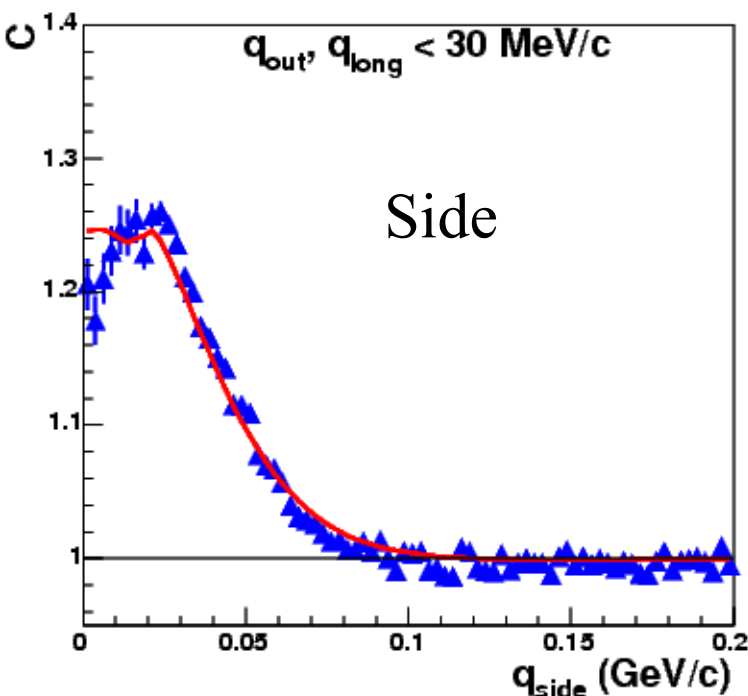
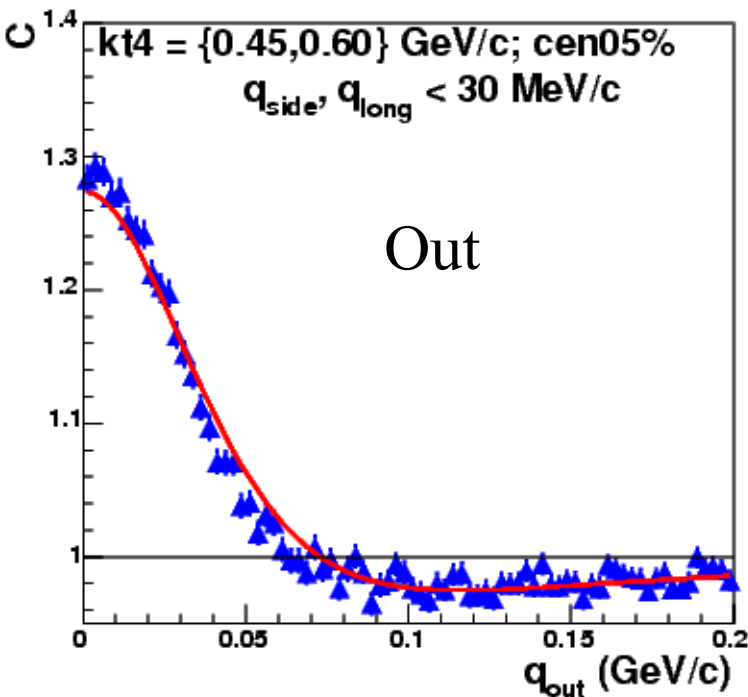
$$\alpha = 1.520 \pm 0.009$$

$$\chi^2/\text{NDF} = 1.11171$$

- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- α parameter increases with k_T
- $\alpha < 2$

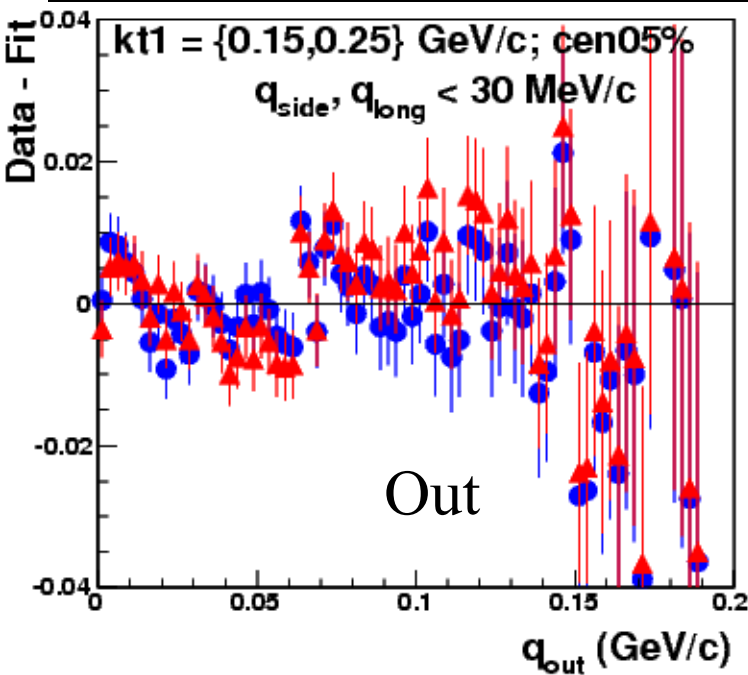


Levy fit to identical $\pi\pi$ correlation function



- λ increases with k_T
- All three radii $R_{o,s,l}$ decrease with k_T
- α parameter increases with k_T
- $\alpha < 2$

Levy source fit vs. Bowler-Sinyukov fit

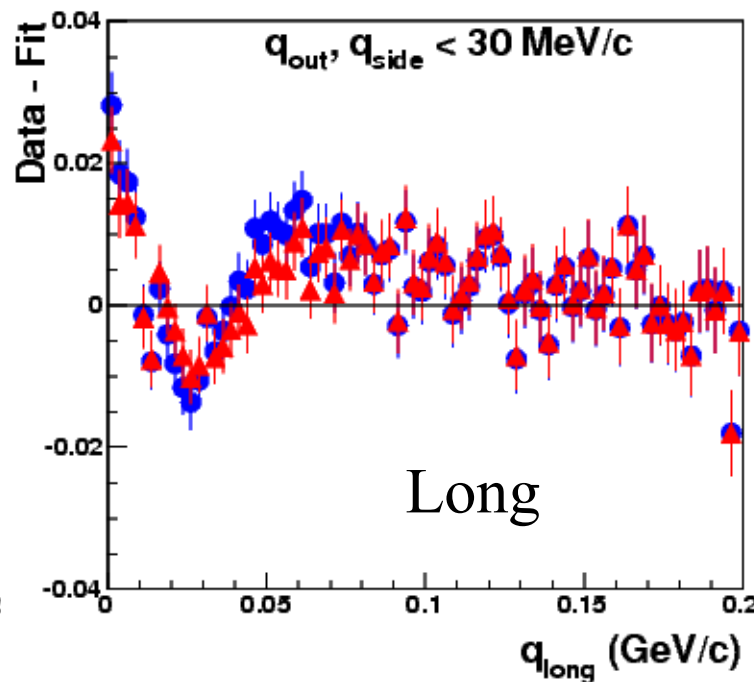
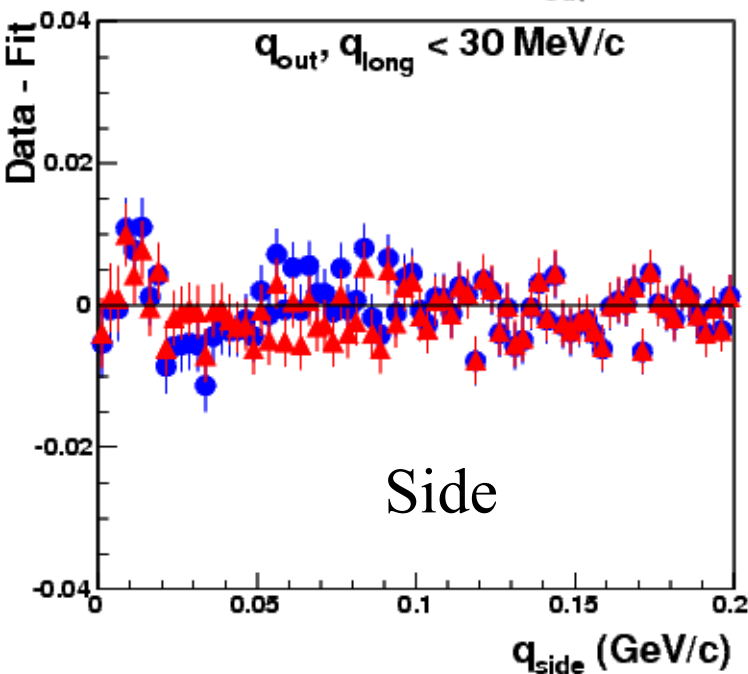


Identical $\pi\pi$ CF (Data - Fit)

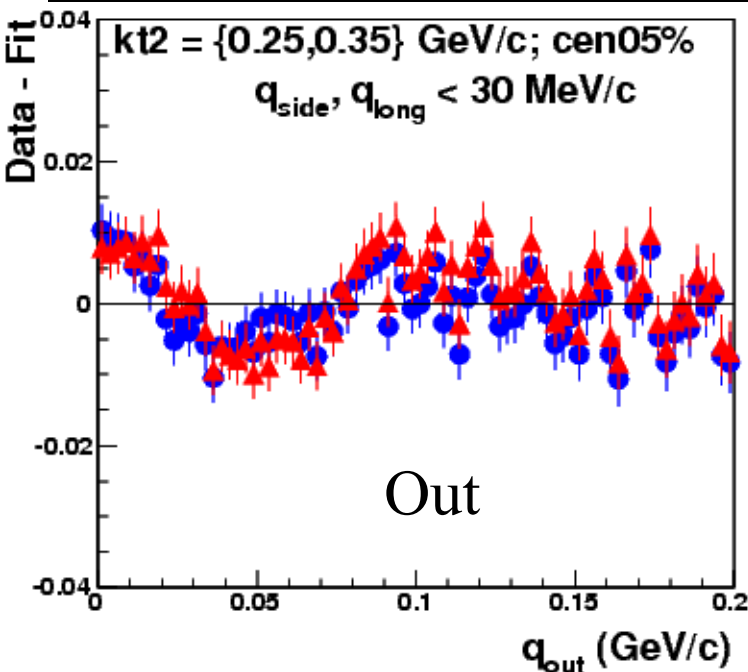
PRELIMINARY Y04

- B-S Gaussian fit
- ▲ B-S fit (Levy)

- Both methods follow the same trend
- Neither is significantly better in fitting 3D experimental CF



Levy source fit vs. Bowler-Sinyukov fit

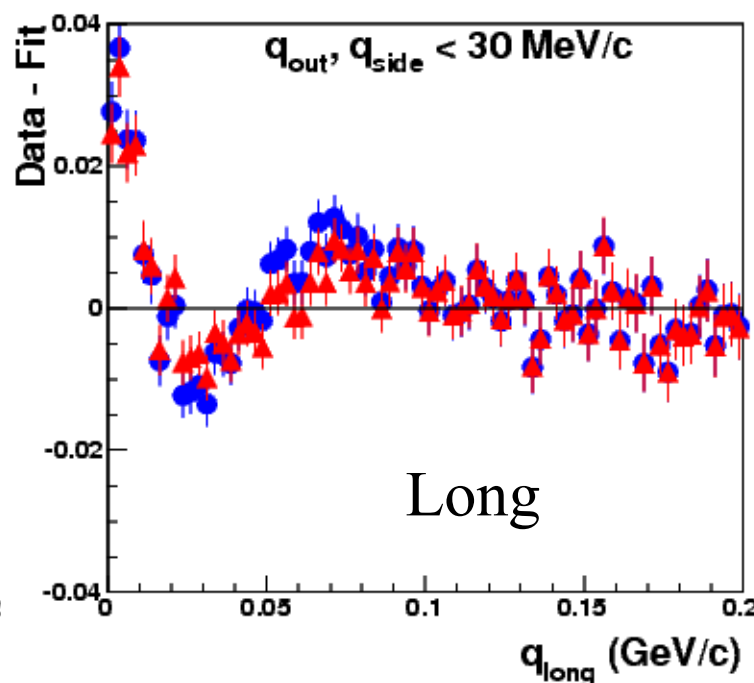
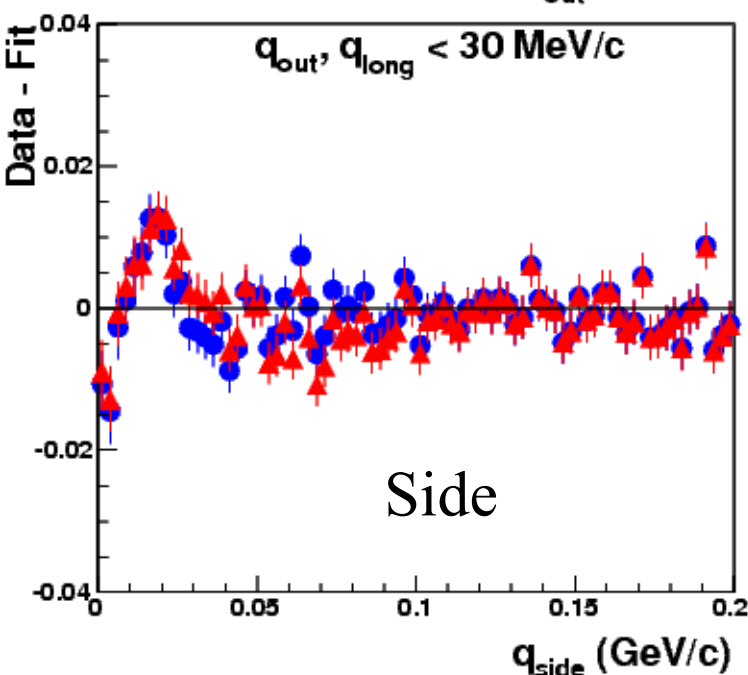


Identical $\pi\pi$ CF (Data - Fit)

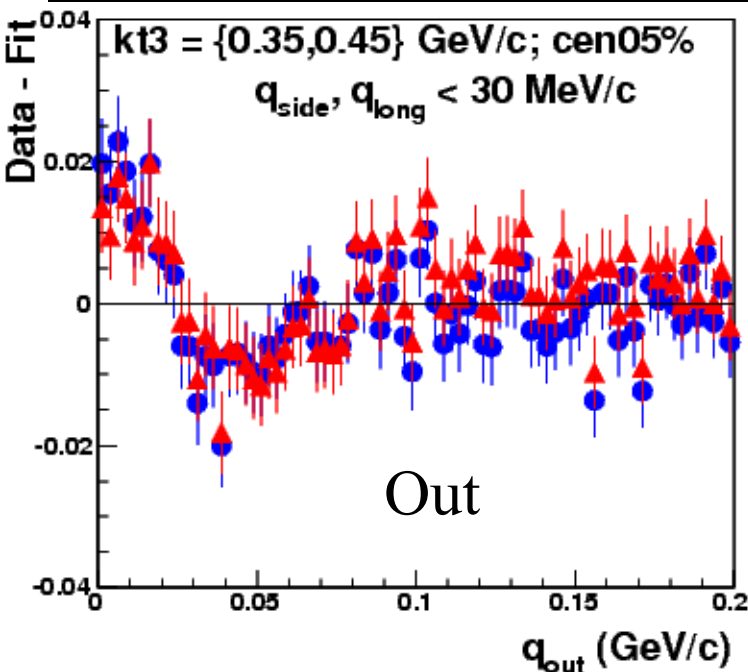
PRELIMINARY Y04

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Levy source fit vs. Bowler-Sinyukov fit

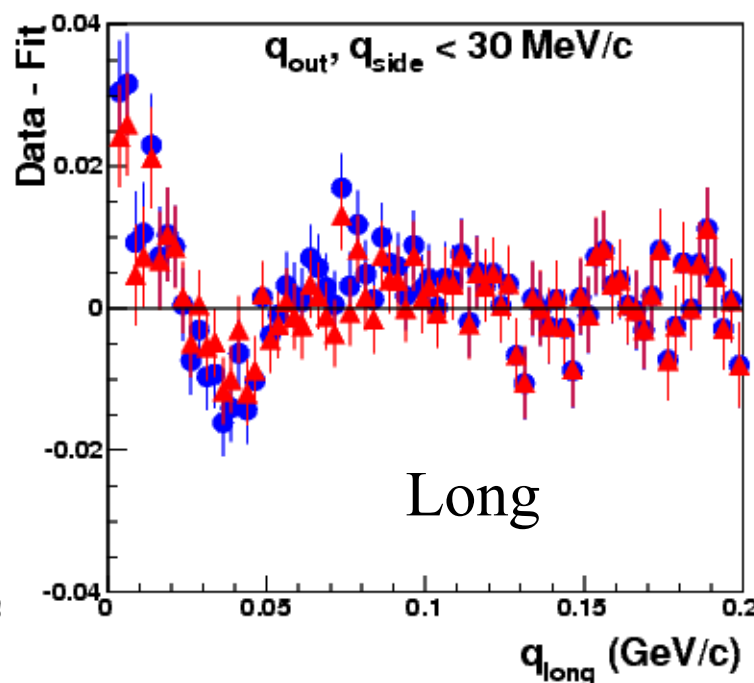
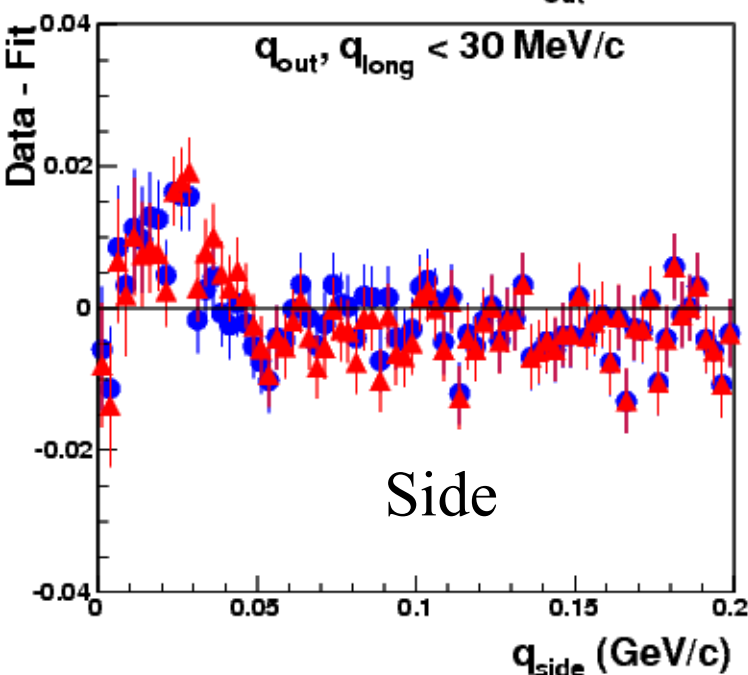


Identical $\pi\pi$ CF (Data - Fit)

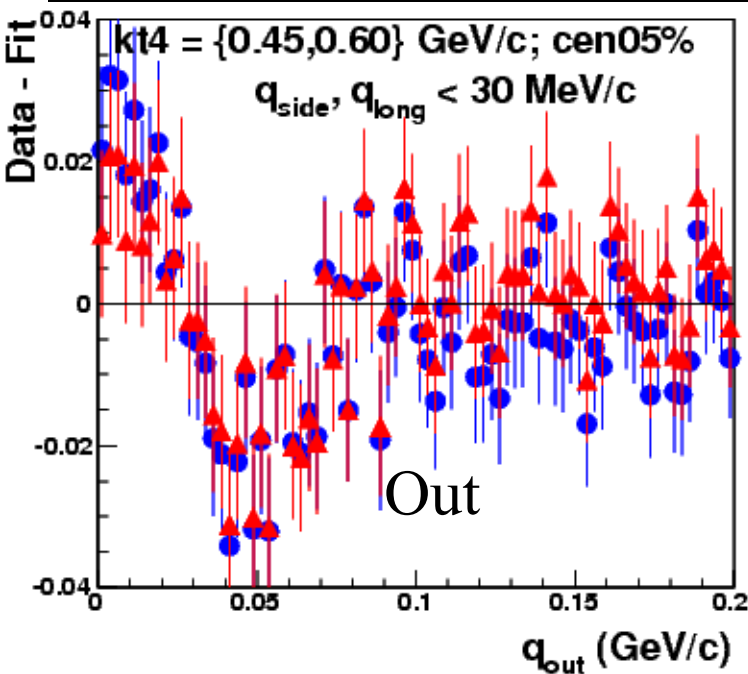
PRELIMINARY Y04

- B-S Gaussian fit
- ▲ B-S fit (Levy)

- Both methods follow the same trend
- Neither is significantly better in fitting 3D experimental CF



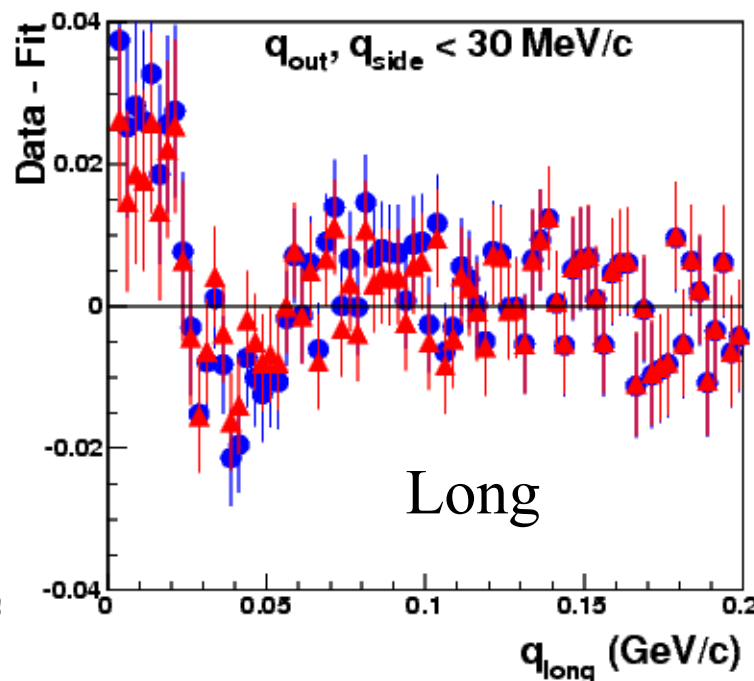
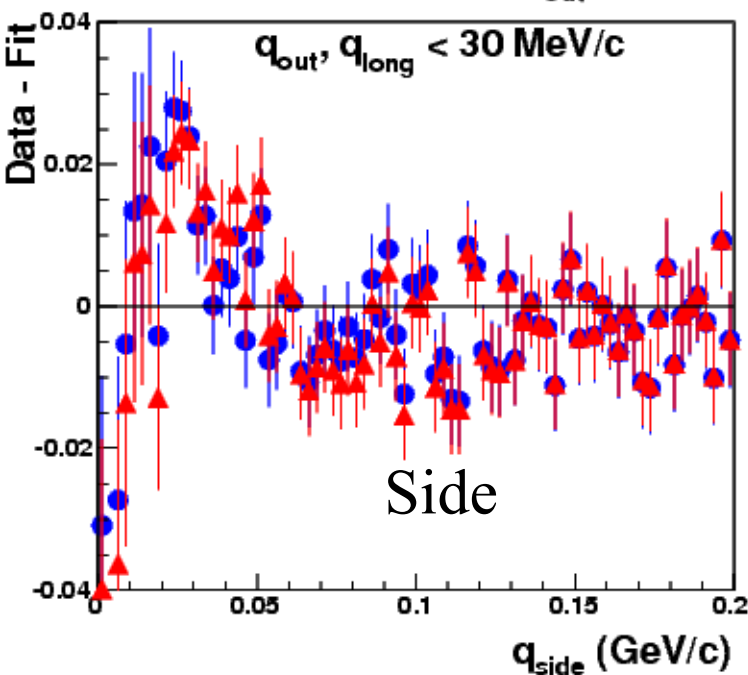
Levy source fit vs. Bowler-Sinyukov fit



Identical $\pi\pi$ CF (Data - Fit)

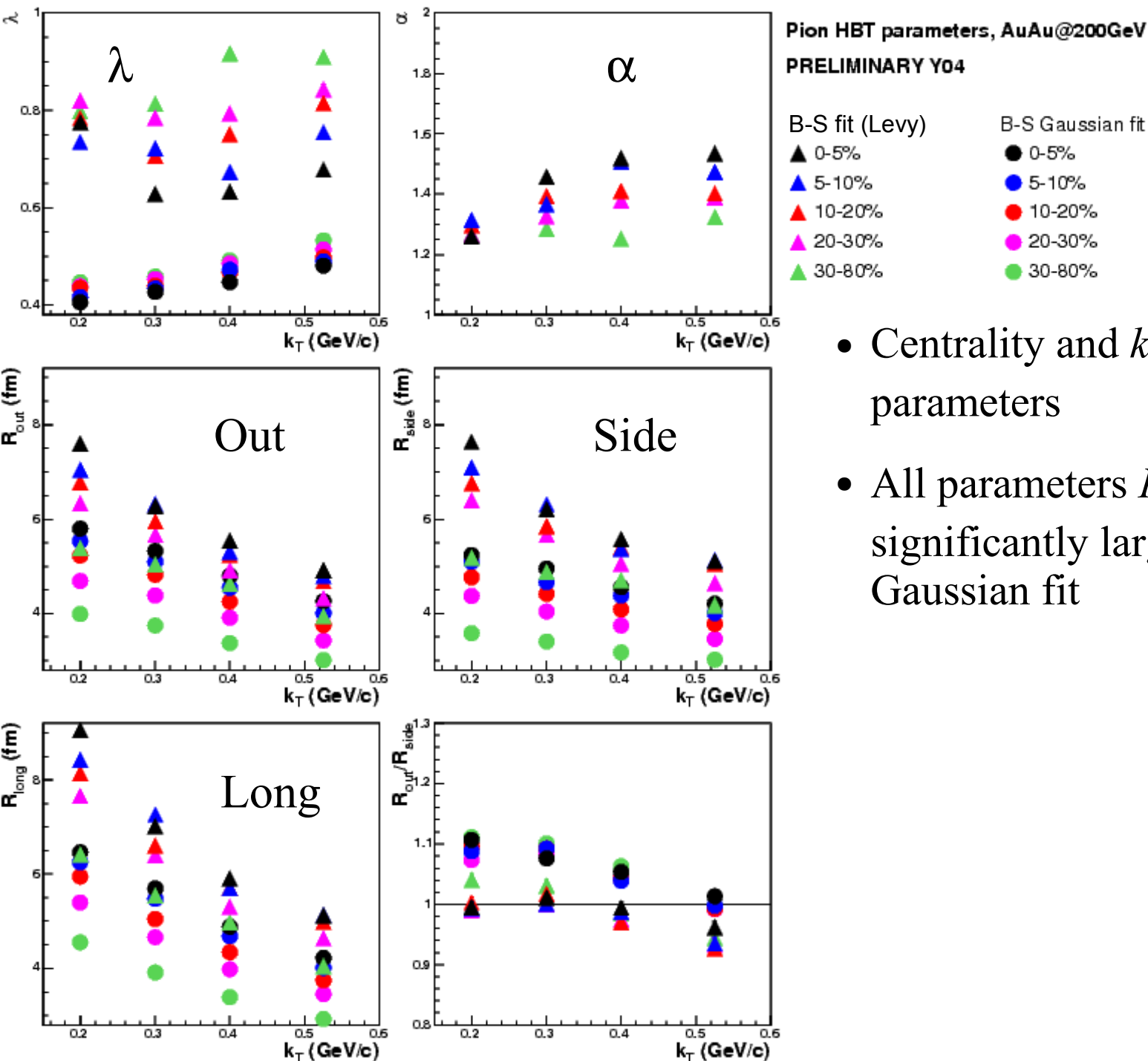
PRELIMINARY Y04

- B-S Gaussian fit
- ▲ B-S fit (Levy)



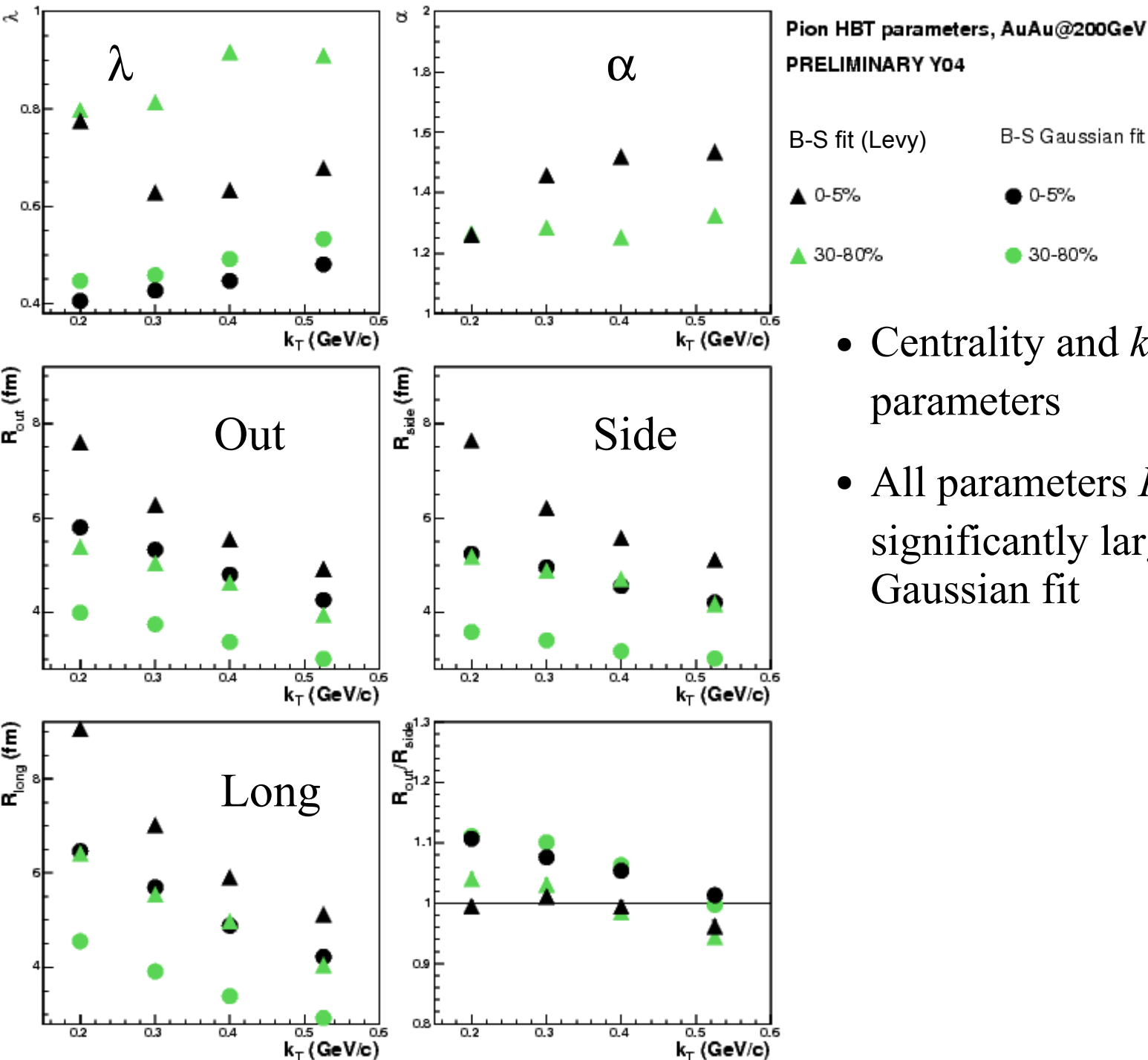
- Both methods follow the same trend
- Neither is significantly better in fitting 3D experimental CF

Levy source fit vs. Bowler-Sinyukov fit



- Centrality and k_T dependence of fit parameters
- All parameters $R_{o,s,l}$ and λ are significantly larger when compared to Gaussian fit

Levy source fit vs. Bowler-Sinyukov fit



- Centrality and k_T dependence of fit parameters
- All parameters $R_{o,s,l}$ and λ are significantly larger when compared to Gaussian fit

Edgeworth expansion

- Method suggested by T.Csörgő, *et al.*, Phys.Lett. B489(2000)15, to study deviations from Gaussian CF
- Edgeworth expansion around 3D Gaussian in B-S procedure

$$\begin{aligned}
 C(q_o, q_s, q_l) = & (1 - \lambda) + \lambda K_{\text{coul}}(q_{\text{inv}}) \\
 & + \lambda K_{\text{coul}}(q_{\text{inv}}) \cdot e^{-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2} \times \\
 & \left[1 + \sum_{n=4, n \text{ even}}^{\infty} \frac{\kappa_{o,n}}{n! (\sqrt{2})^n} H_n(q_o R_o) \right] \times \\
 & \left[1 + \sum_{n=4, n \text{ even}}^{\infty} \frac{\kappa_{s,n}}{n! (\sqrt{2})^n} H_n(q_s R_s) \right] \times \\
 & \left[1 + \sum_{n=4, n \text{ even}}^{\infty} \frac{\kappa_{l,n}}{n! (\sqrt{2})^n} H_n(q_l R_l) \right],
 \end{aligned}$$

- Unable to find the physical interpretation of the fit parameters, it is not clear how to compare extracted parameters to models that assume Gaussian CF

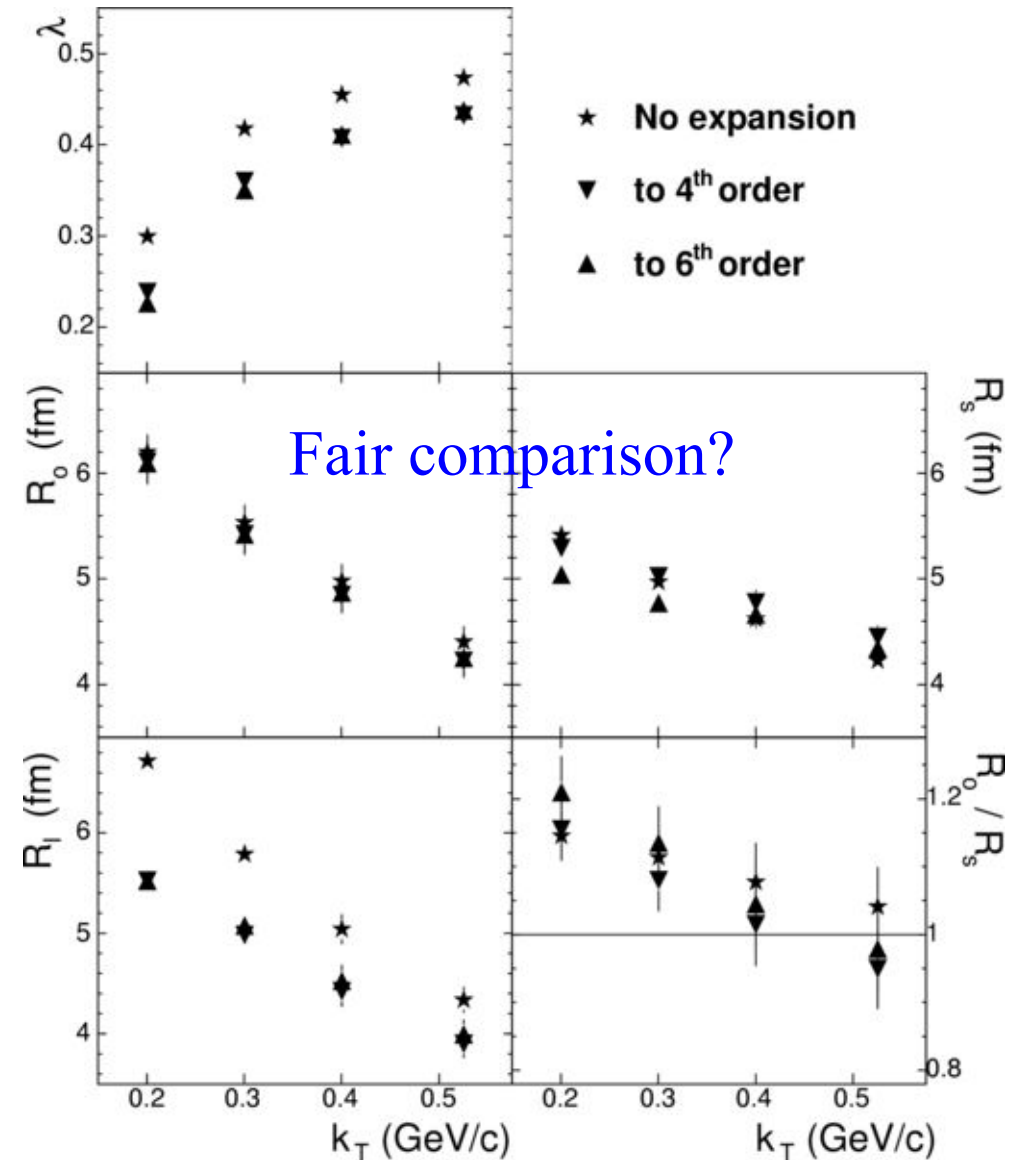
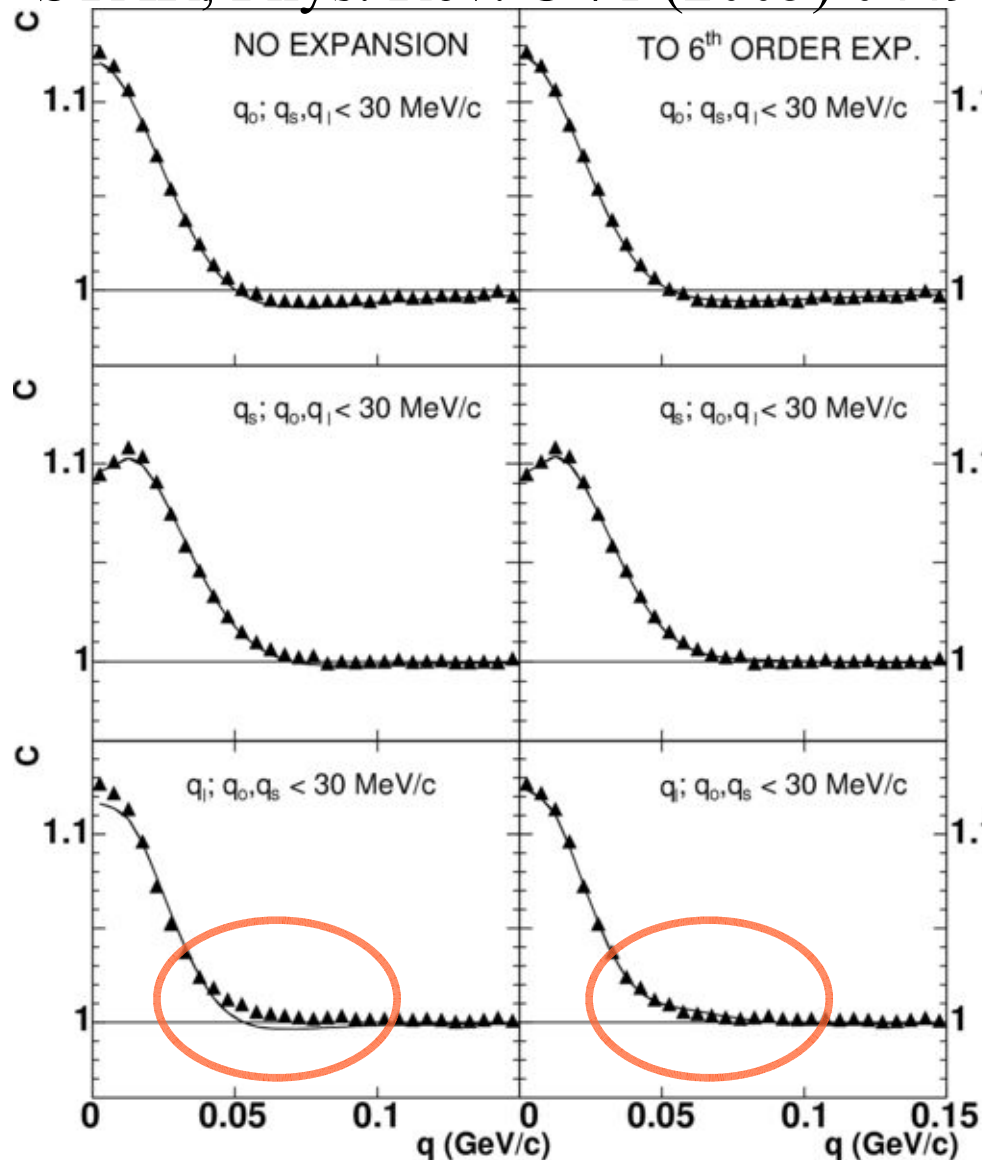
Numbr of parameters

Gaussian	4
4th order	7
6th order	10

Edgeworth expansion fit to identical π - π CF

- Expansion up to 6th order is sufficient.

STAR, Phys. Rev. C 71 (2005) 044906



Summary

- Large statistics of year 2004 data ~ 11 M MinBias Au+Au events at $\sqrt{s_{\text{NN}}} = 200$ GeV, is being processed with the extraction of the k_{T} dependence of interferometry parameters for 5 centrality bins.
- Gaussian fit to experimental CF is consistent within errors with STAR published data.
- Levy source distribution does not fit the experimental CF significantly better when compared to standard Gaussian fit.
- Edgeworth expansion is an improvement but there is no clear interpretation of higher order fit parameters yet.
- It seems that at RHIC Au+Au collisions Gaussian parameterization is sufficient to represent experimental CF.

Thank you

Extra slides

Edgeworth expansion

- Method suggested by T.Csörgő, *et al.*, Phys.Lett. B489(2000)15, to study deviations from Gaussian CF
- Edgeworth expansion around 3D Gaussian in B-S procedure

$$\begin{aligned}
 C(q_o, q_s, q_l) = & (1 - \lambda) + \lambda K_{\text{coul}}(q_{\text{inv}}) \\
 & + \lambda K_{\text{coul}}(q_{\text{inv}}) \cdot e^{-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2} \times \\
 & \left[1 + \sum_{n=4, n \text{ even}}^{\infty} \frac{\kappa_{o,n}}{n!(\sqrt{2})^n} H_n(q_o R_o) \right] \times \\
 & \left[1 + \sum_{n=4, n \text{ even}}^{\infty} \frac{\kappa_{s,n}}{n!(\sqrt{2})^n} H_n(q_s R_s) \right] \times \\
 & \left[1 + \sum_{n=4, n \text{ even}}^{\infty} \frac{\kappa_{l,n}}{n!(\sqrt{2})^n} H_n(q_l R_l) \right],
 \end{aligned}$$

- Unable to find the physical interpretation of the fit parameters, it is not clear how to compare extracted parameters to models that assume Gaussian CF

STAR, Phys. Rev. C 71 (2005) 044906

k_T (MeV/c)	150–250	250–350	350–450	450–600
λ	0.30 ± 0.01	0.42 ± 0.01	0.45 ± 0.01	0.47 ± 0.01
λ (4 th ord.)	0.24 ± 0.01	0.36 ± 0.01	0.41 ± 0.01	0.43 ± 0.01
λ (6 th ord.)	0.23 ± 0.01	0.35 ± 0.01	0.41 ± 0.01	0.44 ± 0.01
R_o	6.16 ± 0.01	5.51 ± 0.01	4.88 ± 0.02	4.32 ± 0.02
R_o (4 th ord.)	6.07 ± 0.04	5.40 ± 0.03	4.75 ± 0.03	4.14 ± 0.04
$\kappa_{o,4}$	0.37 ± 0.05	0.36 ± 0.04	0.33 ± 0.05	0.40 ± 0.06
R_o (6 th ord.)	6.05 ± 0.05	5.40 ± 0.04	4.78 ± 0.04	4.17 ± 0.04
$\kappa_{o,4}$	0.53 ± 0.11	0.45 ± 0.10	0.20 ± 0.11	0.22 ± 0.13
$\kappa_{o,6}$	0.83 ± 0.39	0.53 ± 0.38	0.63 ± 0.44	-0.84 ± 0.53
R_s	5.39 ± 0.01	4.93 ± 0.01	4.53 ± 0.01	4.14 ± 0.02
R_s (4 th ord.)	5.27 ± 0.03	4.98 ± 0.03	4.68 ± 0.03	4.36 ± 0.03
$\kappa_{s,4}$	0.22 ± 0.04	-0.03 ± 0.04	-0.27 ± 0.04	-0.50 ± 0.05
R_s (6 th ord.)	5.01 ± 0.05	4.74 ± 0.04	4.57 ± 0.04	4.26 ± 0.04
$\kappa_{s,4}$	0.99 ± 0.10	0.79 ± 0.10	0.16 ± 0.11	-0.07 ± 0.13
$\kappa_{s,6}$	3.07 ± 0.35	3.21 ± 0.37	1.71 ± 0.44	1.80 ± 0.51
R_l	6.64 ± 0.02	5.72 ± 0.02	4.94 ± 0.02	4.25 ± 0.02
R_l (4 th ord.)	5.47 ± 0.04	4.92 ± 0.03	4.33 ± 0.04	3.82 ± 0.04
$\kappa_{l,4}$	1.60 ± 0.06	1.25 ± 0.05	1.04 ± 0.06	0.78 ± 0.06
R_l (6 th ord.)	5.01 ± 0.05	5.01 ± 0.04	4.43 ± 0.04	3.91 ± 0.04
$\kappa_{l,4}$	1.32 ± 0.07	0.70 ± 0.07	0.54 ± 0.09	0.32 ± 0.11
$\kappa_{l,6}$	-1.76 ± 0.29	-2.82 ± 0.29	-2.41 ± 0.35	-2.12 ± 0.43

Correlation function for two identical bosons

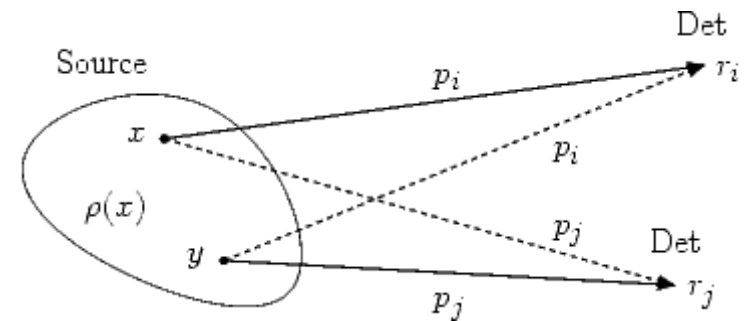
- CF:

$$C_2(p_i, p_j) = \frac{P_2(p_i, p_j)}{P_1(p_i)P_1(p_j)} = 1 + \langle \cos(q \cdot r) \rangle$$

$$q = p_i - p_j$$

$$r = x - y$$

$$k = \frac{1}{2} (p_i + p_j)$$



- Bowler-Sinyukov fit in 3D Bertsch-Pratt parametrization:

$$C_2(\vec{q}, \vec{k}) = (1 - \lambda(\vec{k})) + \lambda(\vec{k}) K_{\text{coul}}(q_{\text{inv}}) \left(1 + \exp \left(-R_{\text{out}}^2(\vec{k}) q_{\text{out}}^2 - R_{\text{side}}^2(\vec{k}) q_{\text{side}}^2 - R_{\text{long}}^2(\vec{k}) q_{\text{long}}^2 - 2R_{\text{outlong}}^2(\vec{k}) q_{\text{out}} q_{\text{long}} \right) \right)$$

$K_{\text{coul}}(q_{\text{inv}})$ = squared Coulomb wavefunction integrated over source $R = 5$ fm

$\lambda(\vec{k})$ = correlation strength, chaoticity

$$q_{\text{out}} = \frac{|\vec{q}_{\text{T}} \cdot \vec{k}_{\text{T}}|}{|\vec{k}_{\text{T}}|}$$

$$q_{\text{side}} = \frac{|\vec{q}_{\text{T}} \times \vec{k}_{\text{T}}|}{|\vec{k}_{\text{T}}|}$$

$$q_{\text{long}} = p_{z,i} - p_{z,j}$$

